



NumPy





Software Application Layers

Domain Specific GUI Applications

Semiconductor, Fluid Dynamics, Seismic Modeling, Financial, etc.

ETS (App construction)

Traits, Chaco, Envisage, Mayavi, etc.

SciPy (Scientific Algorithms)

NumPy (Array Mathematics)

Python

3rd Party Libraries

wxPython

VTK, etc.



IPython



IPython command prompt

- Available at <http://ipython.scipy.org/>
- Fernando Perez, Brian Granger, and others
- Provides a nice environment for scientific computing with Python

```
Python 2.3.3 (#51, Feb 16 2004, 04:07:52) [MSC v.1200 32 bit (Intel)]
Type "copyright", "credits" or "license" for more information.

IPython 0.6.3 -- An enhanced Interactive Python.
?          -> Introduction to IPython's features.
?magic     -> Information about IPython's 'magic' @ functions.
help       -> Python's own help system.
object?    -> Details about 'object'. ?object also works. ?? prints more.

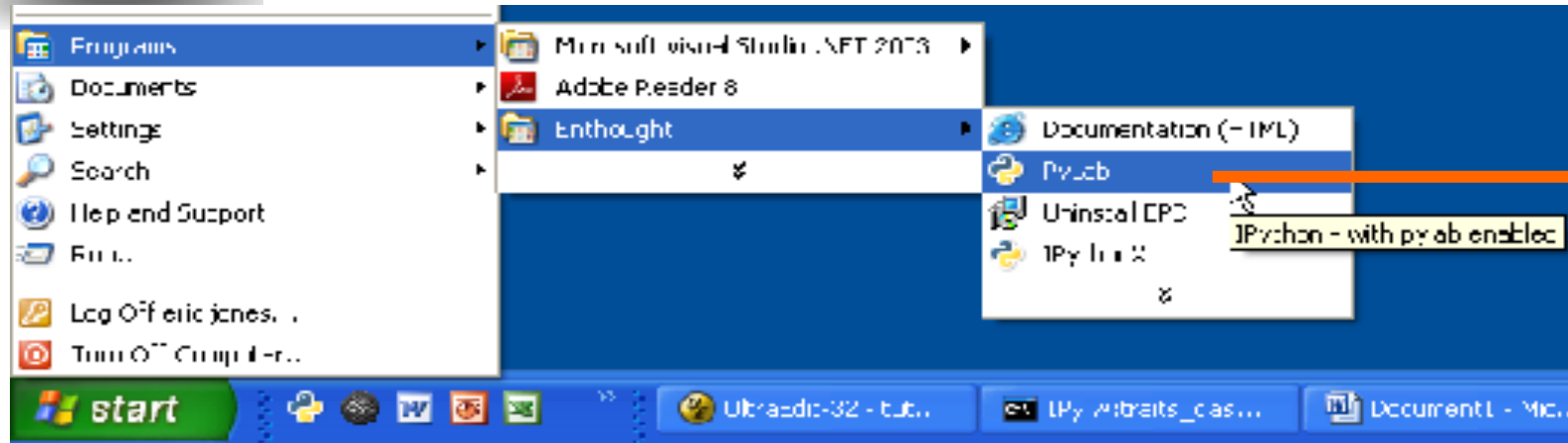
IPython profile: enthought

Welcome to the SciPy Scientific Computing Environment.

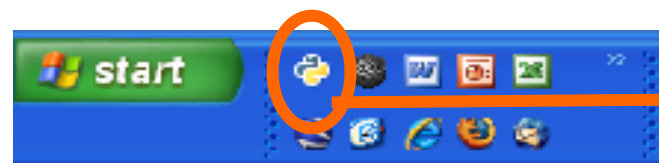
In [1]:
```



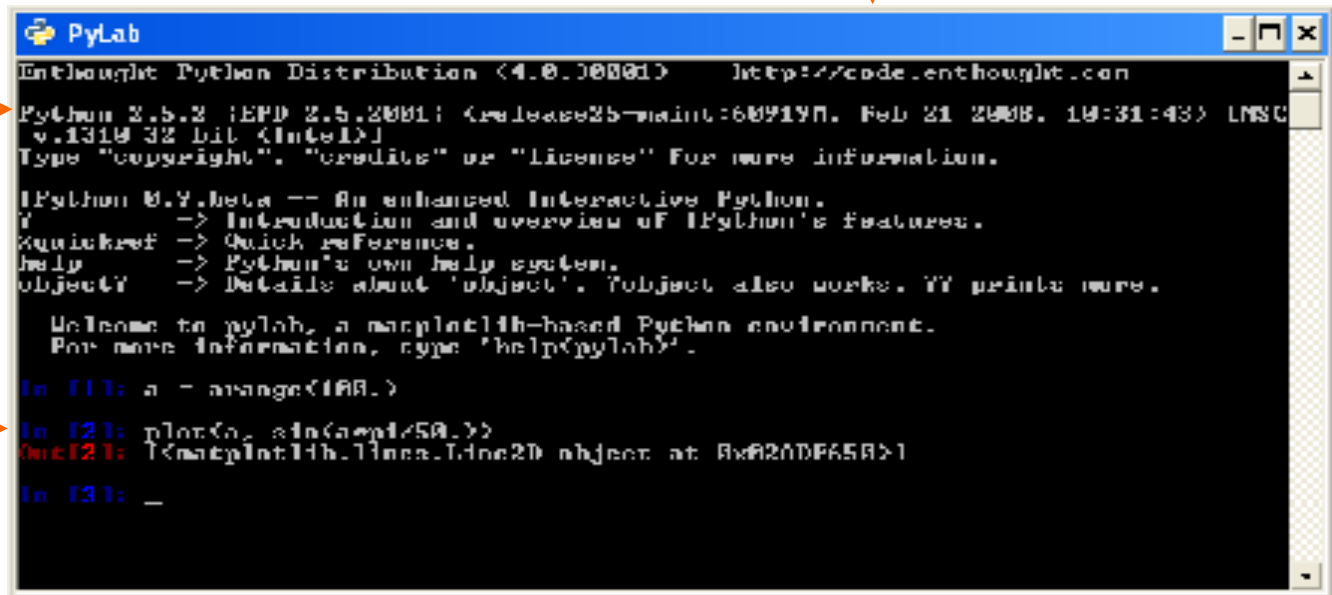
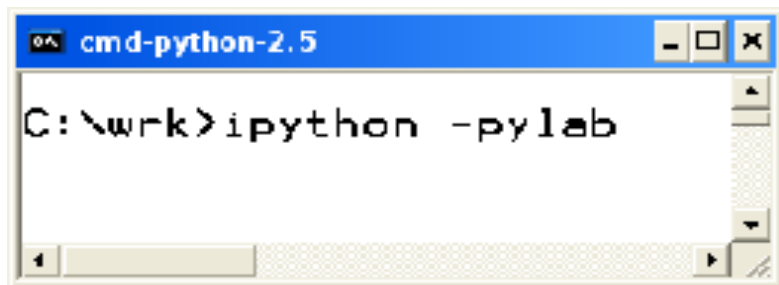
Starting PyLab



or...



or...





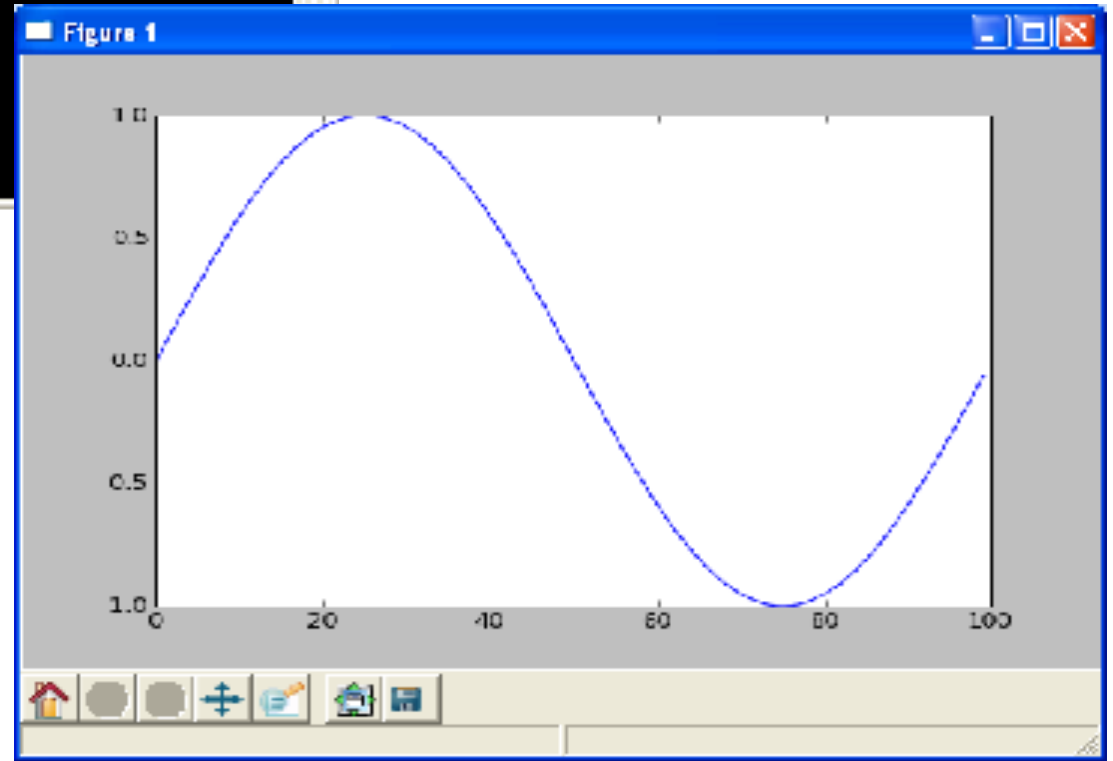
PyLab: Interactive Python Environment

```
PyLab
Enthought Python Distribution (4.0.100001) http://code.enthought.com
Python 2.5.2 (EPD 2.5.2001) (release25-maint:60919M, Feb 21 2008, 18:31:43) [MSC
v.1310 32 bit (Intel)]
Type "copyright", "credits" or "license" for more information.

IPython 0.9.beta -- An enhanced Interactive Python.
?          -> Introduction and overview of IPython's features.
%quickref  -> Quick reference.
help       -> Python's own help system.
object?    -> Details about 'object'. ?object also works, ?? prints more.

Welcome to pylab, a matplotlib-based Python environment.
For more information, type 'help(pylab)'.

In [1]: a = arange(100.)
In [2]: plot(a, sin(ampi/50.))
Out[2]: [matplotlib.lines.Line2D object at 0x02A0E650]
In [3]: _
```



The PyLab mode in IPython handles some gory details behind the scenes. It allows both the Python command interpreter (above) and the GUI plot window (right) to coexist. This involves a bit of multi-threaded magic.

PyLab also imports some handy functions into the command interpreter for user convenience.



IPython

STANDARD PYTHON

```
In [1]: a=1
```

```
In [2]: a
```

```
Out[2]: 1
```

HISTORY COMMAND

```
# List previous commands. Use  
# 'magic' % because 'hist' is  
# histogram function in pylab.
```

```
In [3]: %hist
```

```
1: a=1
```

```
2: a
```

INPUT HISTORY

```
# list string from prompt[2]
```

```
In [4]: _i2
```

```
Out[4]: 'a\n'
```

OUTPUT HISTORY

```
# grab result from prompt[2]
```

```
In [5]: _2
```

```
Out[5]: 1
```

AVAILABLE VARIABLES

```
In [6]: b = [1,2,3]
```

```
# list available variables
```

```
In [7]: whos
```

Variable	Type	Data/Length
a	int	1
b	list	[1, 2, 3]



Directory Navigation

```
# change directory (note Unix style forward slashes!)
```

```
In [9]: cd c:/demo/speed_of_light
```

```
c:\demo\speed_of_light
```

```
# list directory contents
```

```
In [10]: ls
```

```
Volume in drive C has no label.
```

```
Volume Serial Number is 5417-593D
```

```
Directory of c:\demo\speed_of_light
```

```
09/01/2008  02:53 PM  <DIR>          .
09/01/2008  02:53 PM  <DIR>          ..
09/01/2008  02:48 PM                1,188 exercise_speed_of_light.txt
09/01/2008  02:48 PM           2,682,023 measurement_description.pdf
09/01/2008  02:48 PM           187,087 newcomb_experiment.pdf
09/01/2008  02:48 PM                1,312 speed_of_light.dat
09/01/2008  02:48 PM                1,436 speed_of_light.py
09/01/2008  02:48 PM                1,232 speed_of_light2.py
           6 File(s)                2,874,278 bytes
           2 Dir(s) 11,997,437,952 bytes free
```



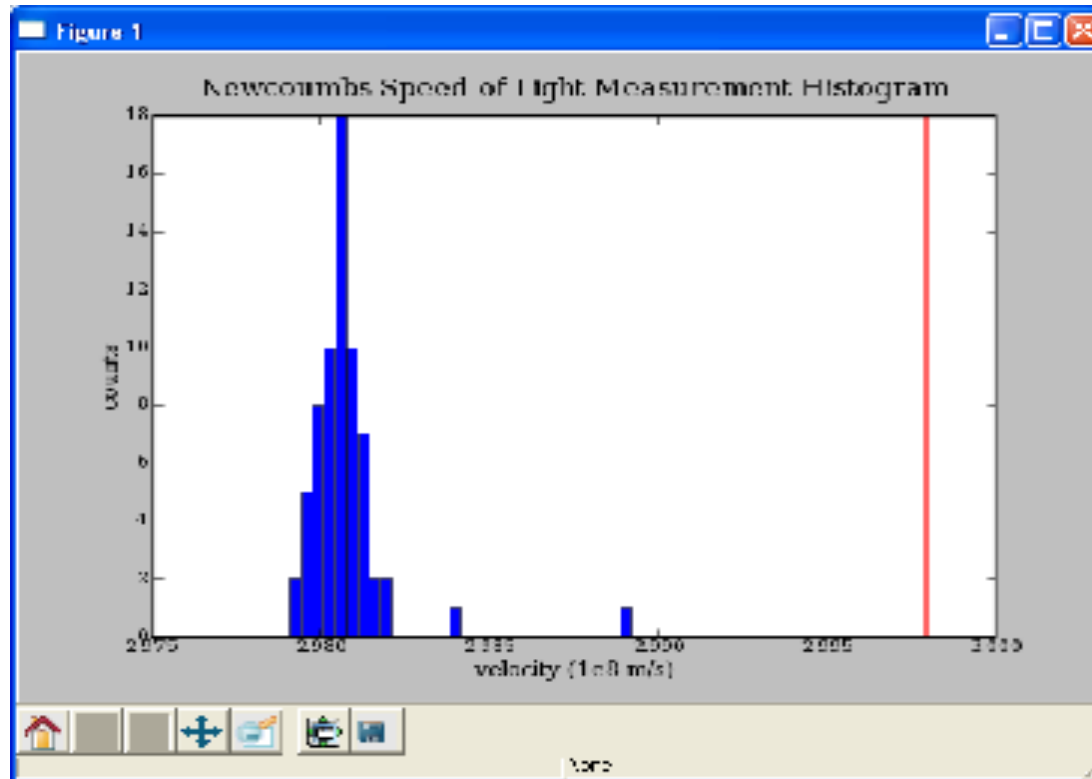

Running Scripts

tab completion

```
In [11]: run speed_of_li  
speed_of_light.dat speed_of_light.py
```

execute a python file

```
In [11]: run speed_of_light.py
```





Function Info -- Magic Commands

HELP USING ?

Follow a command with '?' to print its documentation.

```
In [19]: len?
```

```
Type:          builtin_function_or_method
Base Class:    <type 'builtin_function_or_method'>
String Form:  <built-in function len>
Namespace:    Python builtin
Docstring:
    len(object) -> integer
```

Return the number of items of a sequence or mapping.



Function Info -- Magic Commands

SHOW SOURCE CODE USING ??

Follow a command with '??' to print its source code.

```
In [43]: squeeze??
```

```
def squeeze(a):
```

```
    """Remove single-dimensional entries from the shape of a.
```

```
    Examples
```

```
    -----
```

```
>>> x = array([[[1,1,1],[2,2,2],[3,3,3]])
```

```
>>> x.shape
```

```
(1, 3, 3)
```

```
>>> squeeze(x).shape
```

```
(3, 3)
```

```
    """
```

```
    try:
```

```
        squeeze = a.squeeze
```

```
    except AttributeError:
```

```
        return _wrapit(a, 'squeeze')
```

```
    return squeeze()
```



?? can't show the source code for "extension" functions that are implemented in C.



NumPy and SciPy

SciPy [Scientific Algorithms]

linalg

stats

interpolate

cluster

special

maxentropy

io

fftpack

odr

ndimage

sparse

integrate

signal

optimize

weave

NumPy [Data Structure Core]

fft

random

linalg

NDArray
multi-dimensional
array object

UFunc
fast array
math operations



Helpful Sites

SCIPY DOCUMENTATION PAGE

<http://www.scipy.org/Documentation>

The screenshot shows the SciPy.org website. The top navigation bar includes the SciPy.org logo and the text "Sponsored by ENTHOUGHT". On the left, there is a "Wiki" sidebar with links to "SciPy", "Documentation" (highlighted), "Mailing Lists", "Download", "Installing SciPy", "Typical Software", "Cookbook", "Developer Zone", "Recent Changes", and "Find Page". Below this is a "Page" sidebar with "Immutable Page", "Info", "Attachments", and a "More Actions" dropdown. The main content area is titled "Documentation" and includes a note about installing SciPy and a "Getting Started and Tutorial" section with a link to a FAQ. Below that is a "Numpy" section with a list of resources including a guide to NumPy, a glossary, a tentative tutorial, the Numpy Example List, a database of examples, a summary page, a tutorial for MATLAB users, a tutorial on Record Arrays, and a page on porting to NumPy. Finally, there is a "Scipy" section with a list of resources including a tutorial, a course, a tutorial on interactive data analysis, a history page, MIT tutorials, a scientific computing book, and the example list.

NUMPY EXAMPLES

http://www.scipy.org/Numpy_Example_List_With_Doc

The screenshot shows the "Numpy Example List With Doc" page. It features a "Wiki" sidebar on the left with links to "SciPy", "Documentation", "Mailing Lists", "Download", "Installing SciPy", "Typical Software", "Cookbook", "Developer Zone", "Recent Changes", and "Find Page". The main content area is titled "Numpy Example List With Doc" and includes a note about a generated version of the example list. Below this is a table of contents with links to various example categories: "1. Introduction", "2. Array", "3. Text", "4. Arrays", "5. Record Arrays", "6. Calculus", and "7. FFT".

apply_along_axis()

`numpy.apply_along_axis(func, axis, arr, *args)`

Here the function `func(arr, *args)` returns and `1-d` array. `arr` is an `N-d` array. `axis` varies so as to apply the function along the given axis for each 1-d subarray in `arr`.

Examples:

```

>>> from numpy import *
>>> def myfunc(a):
...     return (a[0]*a**2-1)/2
...
>>> b = array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
>>> apply_along_axis(myfunc, 0, b)
array([[4, 5, 6]])
>>> apply_along_axis(myfunc, -1, b)
array([[2, 3, 4]])

```



Getting Started

IMPORT NUMPY

```
>>> from numpy import *  
>>> __version__  
1.0.2.dev3487
```

or

```
>>> from numpy import array, ...
```

Often at the command line, it is handy to import everything from NumPy into the command shell.

However, if you are writing scripts, it is easier for others to read and debug in the future if you use explicit imports.

USING IPYTHON -PYLAB

```
C:\> ipython -pylab  
In [1]: array((1,2,3))  
Out[1]: array([1, 2, 3])
```

IPython has a 'pylab' mode where it imports all of NumPy, Matplotlib, and SciPy into the namespace for you as a convenience.



While IPython is used for all the demos, '>>>' is used on future slides instead of 'In [1]:' because it takes up less room.



Array Operations

SIMPLE ARRAY MATH

```
>>> a = array([1,2,3,4])
>>> b = array([2,3,4,5])
>>> a + b
array([3, 5, 7, 9])
```

MATH FUNCTIONS

```
# create array from 0 to 10
>>> x = arange(11.)
```

```
# multiply entire array by
# scalar value
```

```
>>> a = (2*pi)/10.
```

```
>>> a
```

```
0.62831853071795862
```

```
>>> a*x
```

```
array([ 0., 0.628, ..., 6.283])
```

```
# in-place operations
```

```
>>> x *= a
```

```
>>> x
```

```
array([ 0., 0.628, ..., 6.283])
```

```
# apply functions to array
```

```
>>> y = sin(x)
```

NumPy defines the following constants:



pi = 3.14159265359

e = 2.71828182846



Introducing NumPy Arrays

SIMPLE ARRAY CREATION

```
>>> a = array([0,1,2,3])
>>> a
array([0, 1, 2, 3])
```

CHECKING THE TYPE

```
>>> type(a)
<type 'numpy.ndarray'>
```

NUMERIC 'TYPE' OF ELEMENTS

```
>>> a.dtype
dtype('int32')
```

BYTES PER ELEMENT

```
>>> a.itemsize
4
```

ARRAY SHAPE

```
# Shape returns a tuple
# listing the length of the
# array along each dimension.
>>> a.shape
(4,)
>>> shape(a)
(4,)
```

ARRAY SIZE

```
# Size reports the entire
# number of elements in an
# array.
>>> a.size
4
>>> size(a)
4
```




Introducing NumPy Arrays

BYTES OF MEMORY USED

```
# Return the number of bytes
# used by the data portion of
# the array.
>>> a.nbytes
16
```

NUMBER OF DIMENSIONS

```
>>> a.ndim
1
```

ARRAY COPY

```
# Create a copy of the array.
>>> b = a.copy()
>>> b
array([0, 1, 2, 3])
```

CONVERSION TO LIST

```
# Convert a NumPy array to a
# Python list.
>>> a.tolist()
[0, 1, 2, 3]

# For 1-D arrays, list
# works equivalently, but
# is slower.
>>> list(a)
[0, 1, 2, 3]
```



Setting Array Elements

ARRAY INDEXING

```
>>> a[0]
0
>>> a[0] = 10
>>> a
[10, 1, 2, 3]
```

FILL

```
# set all values in an array
>>> a.fill(0)
>>> a
[0, 0, 0, 0]

# this also works, but may
# be slower
>>> a[:] = 1
>>> a
[1, 1, 1, 1]
```



BEWARE OF TYPE COERSION

```
>>> a.dtype
dtype('int32')

# assigning a float into
# an int32 array truncates
# the decimal part
>>> a[0] = 10.6
>>> a
[10, 1, 2, 3]

# fill has the same behavior
>>> a.fill(-4.8)
>>> a
[-4, -4, -4, -4]
```



Arrays from ASCII Data

BASIC PATTERN

```
# Read data into a list of lists,  
# and then convert to an array.  
file = open('myfile.txt')  
  
# Create a list for all the data.  
data = []  
  
for line in file:  
    # Read each row of data into a  
    # list of floats.  
    row_data = [float(x) for x in  
                line.split()]  
    # And add this row to the  
    # entire data set.  
    data.append(row_data)  
# Finally, convert the "list of  
# lists" into a 2D array.  
data = array(data)  
f.close()
```

COMMA SEPARATED FILES

```
# The csv module is also handy.  
import csv  
f = open('myfile.txt')  
reader = csv.reader(f)  
  
# Create a list for all the data.  
data = []  
  
# Note that the reader has  
# already done the "split"  
for line in reader:  
    row_data = [float(x) for x in  
                line]  
    data.append(row_data)  
  
# Finally, convert the "list of  
# lists" into a 2D array.  
data = array(data)  
f.close()
```



Slicing

```
var [lower : upper : step]
```

Extracts a portion of a sequence by specifying a lower and upper bound.

The lower-bound element is included, but the upper-bound element is not included.

Mathematically: [lower,upper). The step value specifies the stride between elements.

SLICING LISTS

```
# indices:      0  1  2  3  4
>>> l = array([10,11,12,13,14])
# [10,11,12,13,14]
>>> l[1:3]
[11, 12]
```

```
# negative indices work also
```

```
>>> l[1:-2]
[11, 12]
>>> l[-4:3]
[11, 12]
```

OMITTING INDICES

```
# omitted boundaries are
# assumed to be the beginning
# (or end) of the list
```

```
# grab first three elements
```

```
>>> l[:3]
[10, 11, 12]
```

```
# grab last two elements
```

```
>>> l[-2:]
[13, 14]
```

```
# every other element
```

```
>>> l[::2]
[10, 12, 14]
```



Multi-Dimensional Arrays

MULTI-DIMENSIONAL ARRAYS

```
>>> a = array([[ 0, 1, 2, 3],  
              [10,11,12,13]])
```

```
>>> a  
array([[ 0, 1, 2, 3],  
       [10,11,12,13]])
```

(ROWS,COLUMNS)

```
>>> a.shape
```

```
(2, 4)
```

```
>>> shape(a)
```

```
(2, 4)
```

ELEMENT COUNT

```
>>> a.size
```

```
8
```

```
>>> size(a)
```

```
8
```

NUMBER OF DIMENSIONS

```
>>> a.ndim
```

```
2
```

GET/SET ELEMENTS

```
>>> a[1,3]
```

```
13
```

column
row

```
>>> a[1,3] = -1
```

```
>>> a
```

```
array([[ 0, 1, 2, 3],  
       [10,11,12,-1]])
```

ADDRESS FIRST ROW USING SINGLE INDEX

```
>>> a[1]
```

```
array([10, 11, 12, -1])
```



Array Slicing

SLICING WORKS MUCH LIKE STANDARD PYTHON SLICING

```
>>> a[0,3:5]  
array([3, 4])
```

```
>>> a[4:,4:]  
array([[44, 45],  
       [54, 55]])
```

```
>>> a[:,2]  
array([2, 12, 22, 32, 42, 52])
```

STRIDES ARE ALSO POSSIBLE

```
>>> a[2::2,::2]  
array([[20, 22, 24],  
       [40, 42, 44]])
```

0	1	2	3	4	5
10	11	12	13	14	15
20	21	22	23	24	25
30	31	32	33	34	35
40	41	42	43	44	45
50	51	52	53	54	55



Slices Are References

Slices are references to memory in the original array.

Changing values in a slice also changes the original array.

```
>>> a = array((0,1,2,3,4))

# create a slice containing only the
# last element of a
>>> b = a[2:4]
>>> b
array([2, 3])
>>> b[0] = 10

# changing b changed a!
>>> a
array([ 1,  2, 10,  3,  4])
```



Fancy Indexing

INDEXING BY POSITION

```
>>> a = arange(0,80,10)

# fancy indexing
>>> y = a[[1, 2, -3]]
>>> print y
[10 20 50]

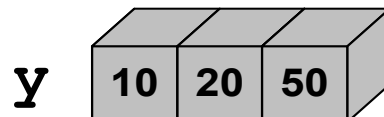
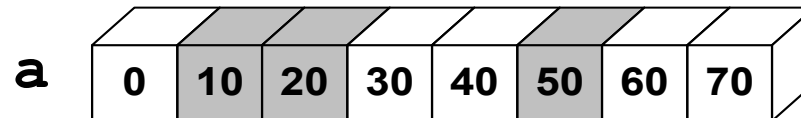
# using take
>>> y = take(a, [1,2,-3])
>>> print y
[10 20 50]
```

INDEXING WITH BOOLEANS

```
>>> mask = array([0,1,1,0,0,1,0,0],
...              dtype=bool)

# fancy indexing
>>> y = a[mask]
>>> print y
[10,20,50]

# using compress
>>> y = compress(mask, a)
>>> print y
[10,20,50]
```





Fancy Indexing in 2-D

```
>>> a[(0,1,2,3,4), (1,2,3,4,5)]  
array([ 1, 12, 23, 34, 45])
```

```
>>> a[3:,[0, 2, 5]]  
array([[30, 32, 35],  
       [40, 42, 45]])  
       [50, 52, 55]])
```

```
>>> mask = array([1,0,1,0,0,1],  
                 dtype=bool)
```

```
>>> a[mask,2]  
array([2,22,52])
```

0	1	2	3	4	5
10	11	12	13	14	15
20	21	22	23	24	25
30	31	32	33	34	35
40	41	42	43	44	45
50	51	52	53	54	55

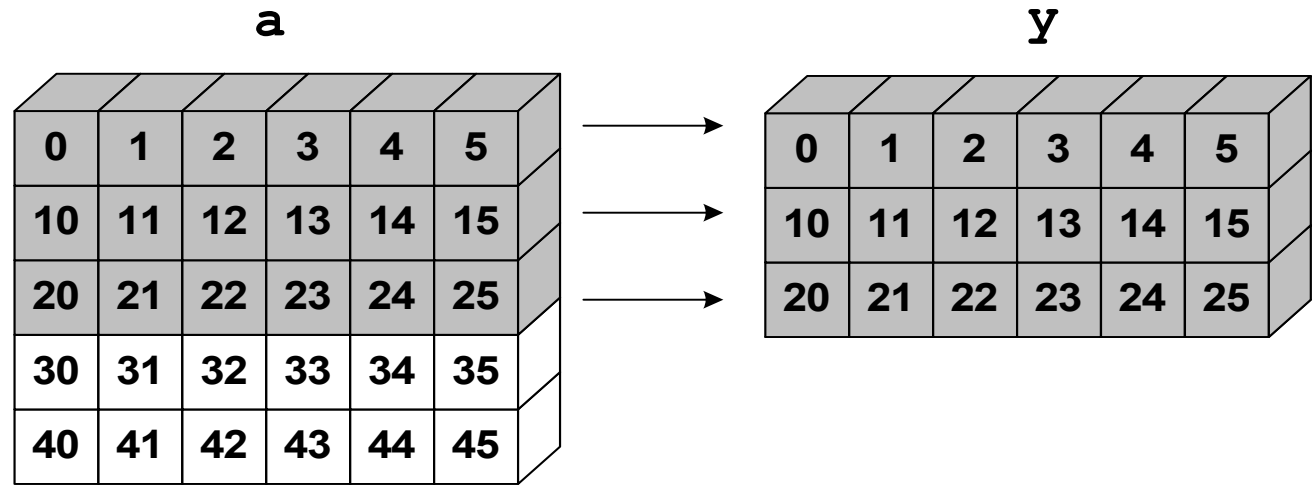


Unlike slicing, fancy indexing creates copies instead of views into original arrays.

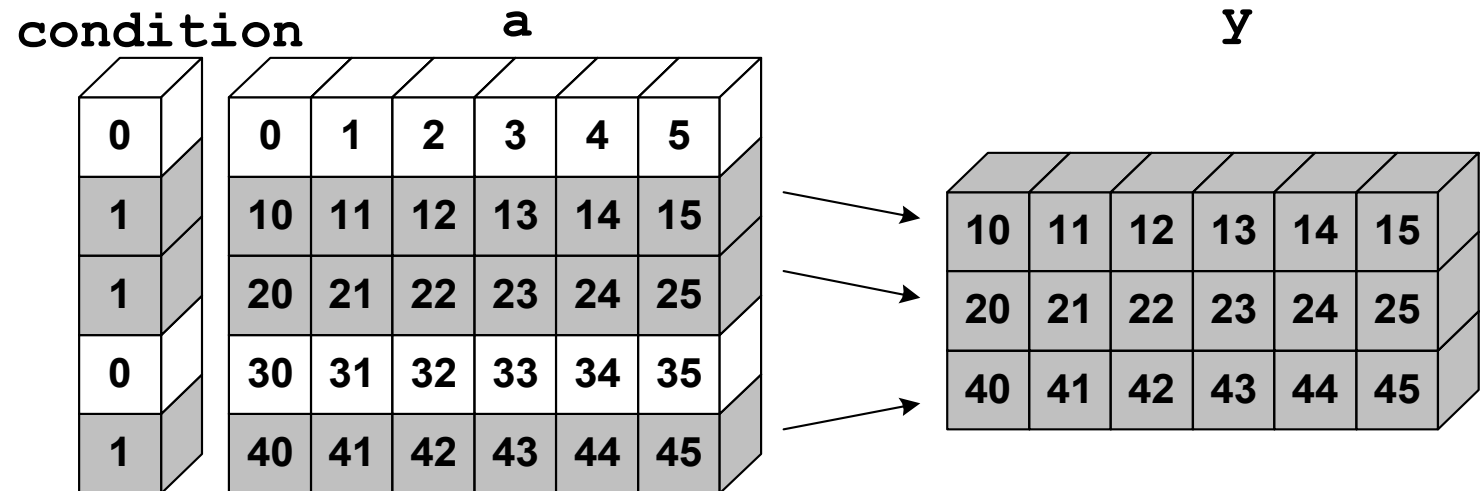


“Incomplete” Indexing

```
>>> y = a[:3]
```



```
>>> y = a[condition]
```

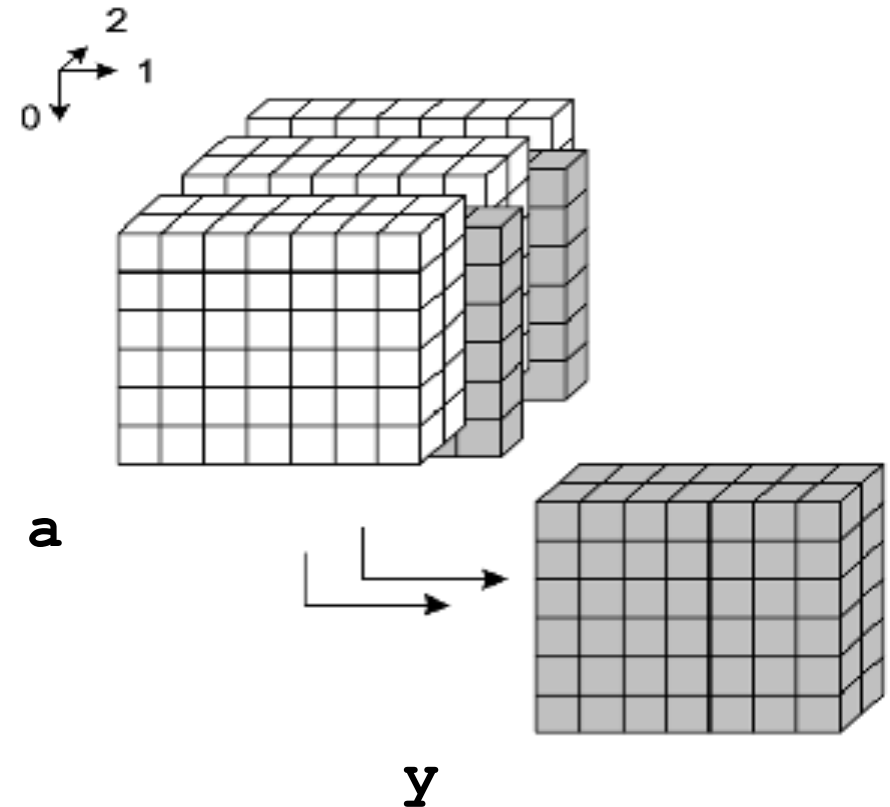




3-D Example

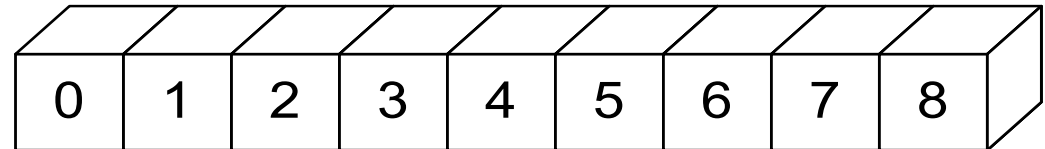
MULTIDIMENSIONAL

```
# retrieve two slices from a  
# 3-D cube via indexing  
>>> y = a[:, :, [2, -2]]  
  
# the take() function also works  
>>> y = take(a, [2, -2], axis=2)
```



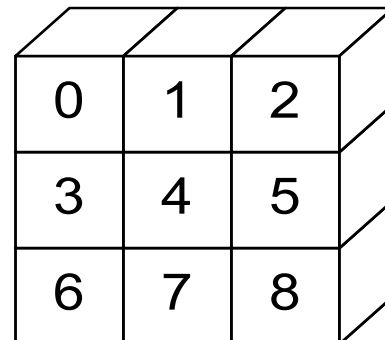


Array Data Structure



Memory block

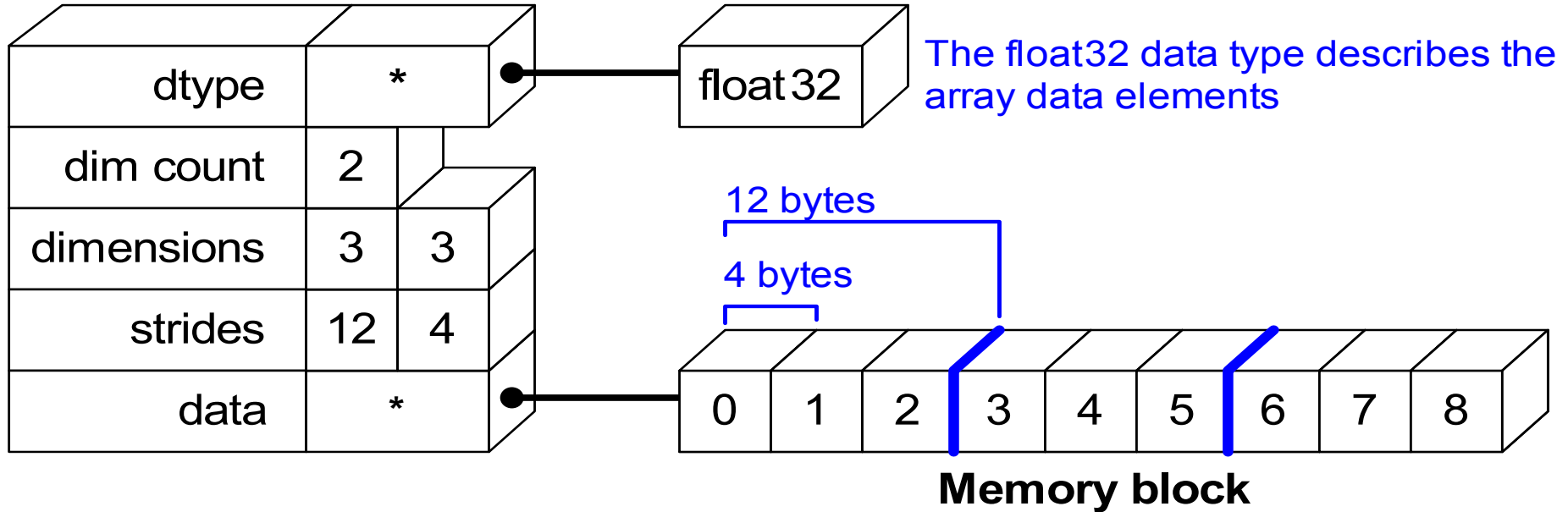
Python View :



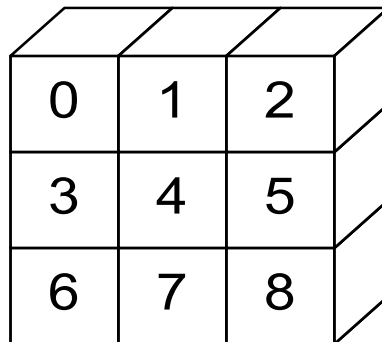


Array Data Structure

NDArray Data Structure



Python View :

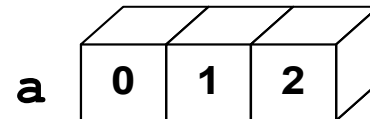




Indexing with None

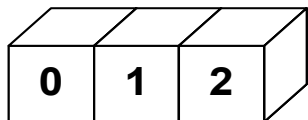
`None` is a special index that inserts a new axis in the array at the specified location.

Each `None` increases the array's dimensionality by 1.



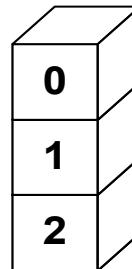
1 X 3

```
>>> y = a[None, :]  
>>> shape(y)  
(1, 3)
```



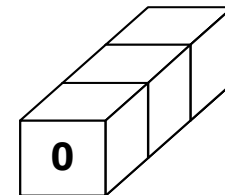
3 X 1

```
>>> y = a[:, None]  
>>> shape(y)  
(3, 1)
```



3 X 1 X 1

```
>>> y = a[:, None, None]  
>>> shape(y)  
(3, 1, 1)
```





NumPy dtypes

Basic Type	Available NumPy types	Comments
Boolean	<code>bool</code>	Elements are 1 byte in size.
Integer	<code>int8, int16, int32, int64, int128, int</code>	<code>int</code> defaults to the size of <code>int</code> in C for the platform.
Unsigned Integer	<code>uint8, uint16, uint32, uint64, uint128, uint</code>	<code>uint</code> defaults to the size of unsigned <code>int</code> in C for the platform.
Float	<code>float32, float64, float, longfloat,</code>	Float is always a double precision floating point value (64 bits). <code>longfloat</code> represents large precision floats. Its size is platform-dependent.
Complex	<code>complex64, complex128, complex</code>	The real and complex elements of a <code>complex64</code> are each represented by a single precision (32 bit) value for a total size of 64 bits.
Strings	<code>str, unicode</code>	
Object	<code>object</code>	Represent items in array as Python objects.
Records	<code>void</code>	Used for arbitrary data structures.



Summary of (most) array attributes/ methods

BASIC ATTRIBUTES

`a.dtype` - Numerical type of array elements: `float32`, `uint8`, etc.

`a.shape` - Shape of the array. `(m,n,o,...)`

`a.size` - Number of elements in entire array

`a.itemsize` - Number of bytes used by a single element in the array

`a.nbytes` - Number of bytes used by entire array (data only)

`a.ndim` - Number of dimensions in the array



Summary of (most) array attributes/methods

SHAPE OPERATIONS

`a.flat` - An iterator to step through array as if it is 1-D

`a.flatten()` - Returns a 1-D copy of a multi-dimensional array

`a.ravel()` - Same as `flatten()`, but returns a 'view' if possible

`a.resize(new_size)` - Changes the size/shape of an array in place

`a.swapaxes(axis1, axis2)` - Swaps the order of two axes in an array

`a.transpose(*axes)` - Swaps the order of any number of array axes `a.T` -

Shorthand for `a.transpose()`

`a.squeeze()` - Removes any `length==1` dimensions from an array



Summary of (most) array attributes/ methods

FILL AND COPY

- `a.copy()` - Returns a copy of the array
- `a.fill(value)` - Fills array with a scalar value

CONVERSION / COERCION

- `a.tolist()` - Converts array into nested lists of values
- `a.tostring()` - Raw copy of array memory into a Python string
- `a.astype(dtype)` - Returns array coerced to the given dtype
- `a.byteswap(False)` - Converts byte order (big \leftrightarrow little endian)
- `a.view(type_or_dtype)` - Creates new ndarray that sees the
the same memory but interprets it as
a new data-type (or subclass of ndarray)



Summary of (most) array attributes/methods

COMPLEX NUMBERS

`a.real` - Returns the real part of the array

`a.imag` - Returns the imaginary part of the array

`a.conjugate()` - Returns the complex conjugate of the array

`a.conj()` - Returns the complex conjugate of an array.

(same as `conjugate`)



Summary of (most) array attributes/ methods

SAVING

`a.dump(file)` - Stores a binary array data out to the given file
`a.dumps()` - Returns the binary pickle of the array as a string
`a.tofile(fid, sep="", format="%s")` - Formatted ASCII output to file

SEARCH / SORT

`a.nonzero()` - Returns indices for all non-zero elements in a
`a.sort(axis=-1)` - In-place sort of array elements along axis
`a.argsort(axis=-1)` - Returns indices for element sort order along axis
`a.searchsorted(b)` - Returns index where elements from b would go in a

ELEMENT MATH OPERATIONS

`a.clip(low, high)` - Limits values in array to the specified range
`a.round(decimals=0)` - Rounds to the specified number of digits
`a.cumsum(axis=None)` - Cumulative sum of elements along axis
`a.cumprod(axis=None)` - Cumulative product of elements along axis



Summary of (most) array attributes/ methods

REDUCTION METHODS

All the following methods “reduce” the size of the array by 1 dimension by carrying out an operation along the specified axis. If axis is None, the operation is carried out across the entire array.

`a.sum(axis=None)` - Sums up values along axis

`a.prod(axis=None)` - Finds the product of all values along axis

`a.min(axis=None)` - Finds the minimum value along axis

`a.max(axis=None)` - Finds the maximum value along axis

`a.argmin(axis=None)` - Finds the index of the minimum value along axis

`a.argmax(axis=None)` - Finds the index of the maximum value along axis

`a.ptp(axis=None)` - Calculates `a.max(axis) - a.min(axis)`

`a.mean(axis=None)` - Finds the mean (average) value along axis

`a.std(axis=None)` - Finds the standard deviation along axis

`a.var(axis=None)` - Finds the variance along axis

`a.any(axis=None)` - True if any value along axis is non-zero (or)

`a.all(axis=None)` - True if all values along axis are non-zero (and)



Matrix Objects

MATRIX CREATION

```
# Matlab-like creation from string
```

```
>>> A = mat('1,2,4;2,5,3;7,8,9')
```

```
>>> print A
```

```
Matrix([[1, 2, 4],  
        [2, 5, 3],  
        [7, 8, 9]])
```

```
# matrix exponents
```

```
>>> print A**4
```

```
Matrix([[ 6497,   9580,   9836],  
        [ 7138, 10561, 10818],  
        [18434, 27220, 27945]])
```

```
# matrix multiplication
```

```
>>> print A*A.I
```

```
Matrix([[ 1.,  0.,  0.],  
        [ 0.,  1.,  0.],  
        [ 0.,  0.,  1.]])
```

BMAT

```
# create a matrix from
```

```
# sub-matrices
```

```
>>> a = array([[1,2],  
              [3,4]])
```

```
>>> b = array([[10,20],  
              [30,40]])
```

```
>>> bmat('a,b;b,a')
```

```
matrix([[ 1,  2, 10, 20],  
        [ 3,  4, 30, 40],  
        [10, 20,  1,  2],  
        [30, 40,  3,  4]])
```



Vectorizing Functions

SCALAR SINC FUNCTION

```
# special.sinc already available
# This is just for show.
def sinc(x):
    if x == 0.0:
        return 1.0
    else:
        w = pi*x
        return sin(w) / w
```

attempt

```
>>> x = array((1.3, 1.5))
>>> sinc(x)
```

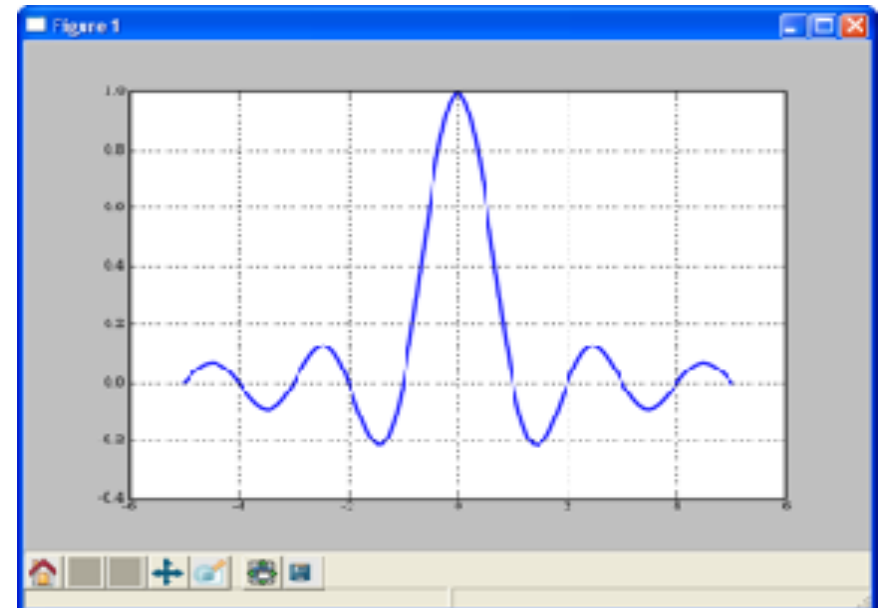
ValueError: The truth value of an array with more than one element is ambiguous. Use a.any() or a.all()

```
>>> x = r_[-5:5:100j]
>>> y = vsinc(x)
>>> plot(x, y)
```

SOLUTION

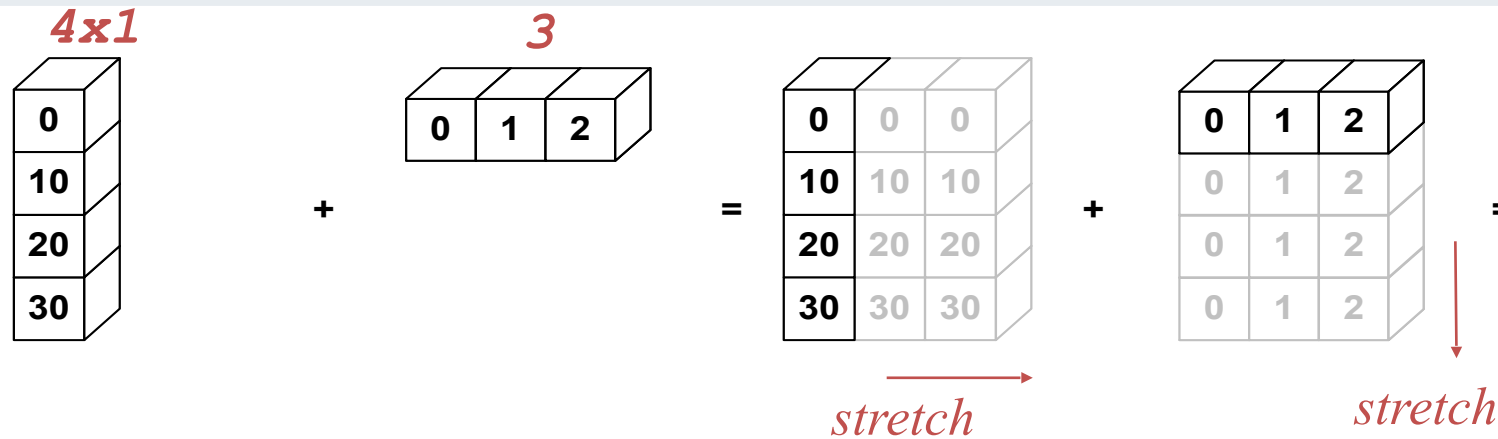
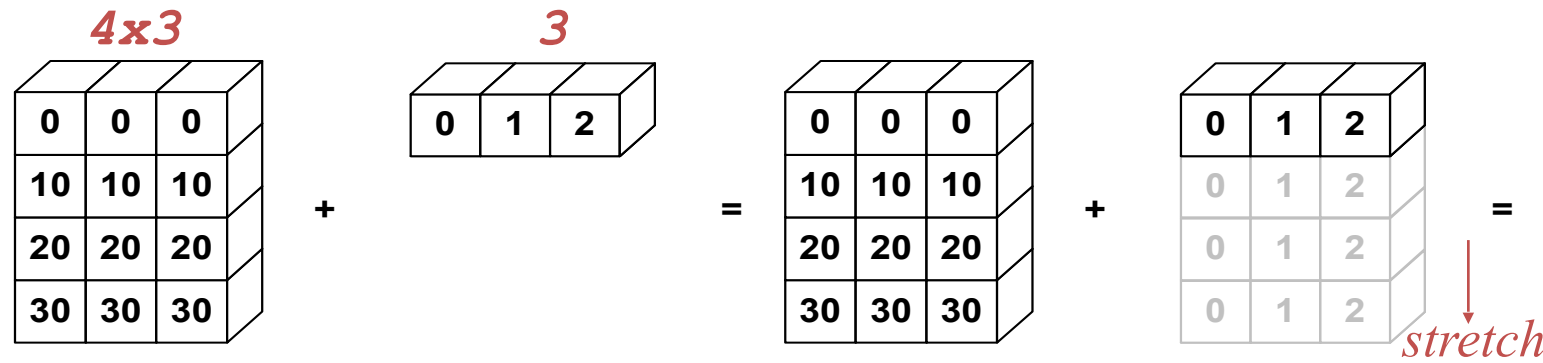
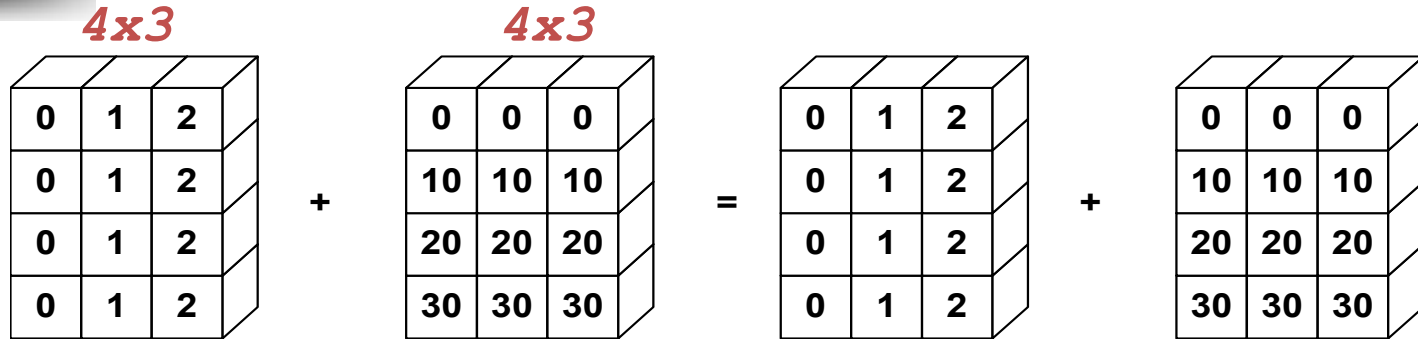
```
>>> from numpy import vectorize
>>> vsinc = vectorize(sinc)
>>> vsinc(x)
array([-0.1981, -0.2122])
```

```
>>> x2 = linspace(-5, 5, 101)
>>> plot(x2, sinc(x2))
```





Array Broadcasting

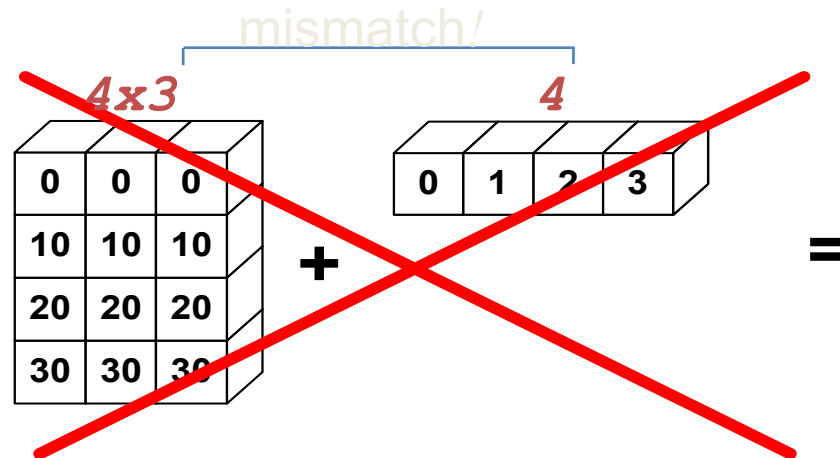




Broadcasting Rules

The trailing axes of both arrays must be either 1 or have the same size for broadcasting to occur. Otherwise, a

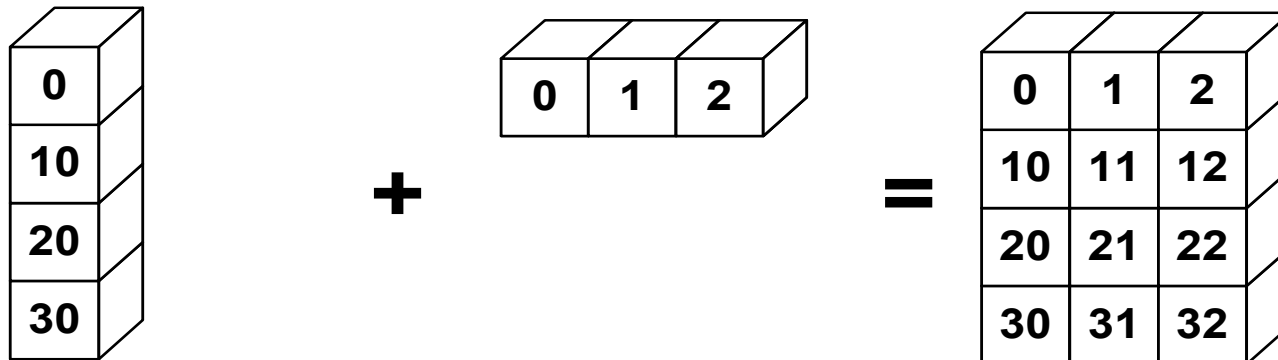
"`ValueError: frames are not aligned`" exception is thrown.





Broadcasting in Action

```
>>> a = array((0,10,20,30))  
>>> b = array((0,1,2))  
>>> y = a[:, None] + b
```





Broadcasting Indices

Broadcasting can also be used to slice elements from different “depths” in a 3-D (or any other shape) array. This is a *very* powerful feature of indexing.

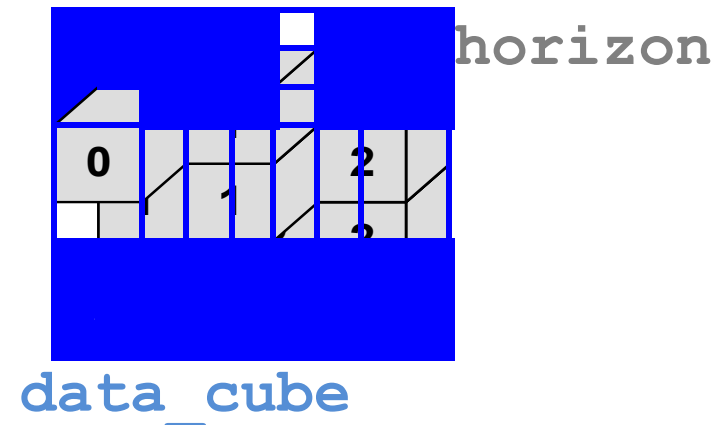
```
>>> xi, yi = ogrid[:3, :3]
>>> zi = array([[0, 1, 2],
                [1, 1, 2],
                [2, 2, 2]])
>>> horizon = data_cube[xi, yi, zi]
```

Indices

	yi	0	1	2
xi	0	0	1	2
	1	1	1	2
	2	2	2	2

zi

Selected Data





Controlling Output Format

```
set_printoptions (precision=None, threshold=None,  
                  edgeitems=None, linewidth=None,  
                  suppress=None)
```

- precision** The number of digits of precision to use for floating point output. The default is 8.
- threshold** Array length where NumPy starts truncating the output and prints only the beginning and end of the array. The default is 1000.
- edgeitems** Number of array elements to print at beginning and end of array when threshold is exceeded. The default is 3.
- linewidth** Characters to print per line of output. The default is 75.
- suppress** Indicates whether NumPy suppresses printing small floating point values in scientific notation. The default is **False**.



Controlling Output Formats

PRECISION

```
>>> a = arange(1e6)
```

```
>>> a
```

```
array([ 0.00000000e+00, 1.00000000e+00, 2.00000000e+00, ...,
        9.99997000e+05, 9.99998000e+05, 9.99999000e+05])
```

```
>>> set_printoptions(precision=3)
```

```
array([ 0.000e+00, 1.000e+00, 2.000e+00, ...,
        1.000e+06, 1.000e+06, 1.000e+06])
```



Controlling Output Formats

SUPPRESSING SMALL NUMBERS

```
>>> set_printoptions(precision=8)
>>> a = array((1, 2, 3, 1e-15))
>>> a
array([ 1.00000000e+00,  2.00000000e+00,  3.00000000e+00,
        1.00000000e-15])
>>> set_printoptions(suppress=True)
>>> a
array([ 1.,  2.,  3.,  0.]
```



Controlling Error Handling

```
seterr(all=None, divide=None, over=None,  
under=None, invalid=None)
```

Set the error handling flags in ufunc operations on a per thread basis. Each of the keyword arguments can be set to 'ignore', 'warn', 'print', 'log', 'raise', or 'call'.

all	All error types to the specified value
divide	'Divide-by-zero' errors
over	'Overflow' errors
under	'Underflow' errors
invalid	'Invalid' floating point errors



Controlling Error Handling

```
>>> a = array((1,2,3))
```

```
>>> a/0.
```

```
Warning: divide by zero encountered in divide
```

```
array([ 1. #INF0000e+000,  1. #INF0000e+000,  1. #INF0000e+000])
```

```
# Ignore division-by-zero. Also, save old values so that  
# we can restore them.
```

```
>>> old_err = seterr(divide='ignore')
```

```
>>> a/0.
```

```
array([ 1. #INF0000e+000,  1. #INF0000e+000,  1. #INF0000e+000])
```




Controlling Error Handling

```
# Restore original error handling mode.  
>>> old_err  
{'divide': 'print', 'invalid': 'print', 'over':  
  'print', 'under': 'ignore'}  
>>> seterr(**old_err)  
>>> a/0.  
Warning: divide by zero encountered in divide  
array([ 1. #INF0000e+000,  1. #INF0000e+000,  
       1. #INF0000e+000])
```



“Structured” Arrays

Elements of an array can be any fixed-size data structure!

```
name char[10]
age int
weight double
```

Brad	Jane	John	Fred
33	25	47	54
135.0	105.0	225.0	140.0
Henry	George	Brian	Amy
29	61	32	27
154.0	202.0	137.0	187.0
Ron	Susan	Jennifer	Jill
19	33	18	54
188.0	135.0	88.0	145.0

EXAMPLE

```
>>> from numpy import dtype, empty
# structured data format
>>> fmt = dtype([('name', 'S10'),
                ('age', int),
                ('weight', float)
                ])
>>> a = empty((3,4), dtype=fmt)
>>> a.itemsize
22
>>> a['name'] = [['Brad', ... , 'Jill']]
>>> a['age'] = [[33, ... , 54]]
>>> a['weight'] = [[135, ... , 145]]
>>> print a
[(['Brad', 33, 135.0)
 ...
 ('Jill', 54, 145.0)]]
```



Structured Arrays

```
import numpy as np
format = np.dtype([('symbol', 'S4'),
                  ('date', 'O'),
                  ('open', 'f8'),
                  ('close', 'f8'),
                  ('low', 'f8'),
                  ('high', 'f8'),
                  ('adj_close',
                   'f8'),
                  ('volume', 'i4')])
r = np.array(<data>, dtype=format)
r = r.view(np.recarray)
query1 = r[r.volume > 1e8]
print query1.symbol
print query1.date
query2 = r[r.close > 1.05*r.open]
print query2.symbol
print query2.date
mask = (r.close - r.open) >
0.10*r.open
query3 = r[mask]
```

Symbol	Date	Open	Close	...	Volume
GOOG	7/19/07	553.46	548.59	...	11127200
QQQQ	7/19/07	50.41	50.32	...	116563800
GE	7/19/07	40.58	40.71	...	29766400
AAPL	7/19/07	140.3	140.0	...	26174700
YHOO	7/19/07	26.32	26.03	...	29537900
MSFT	7/19/07	31.05	31.51	...	121159300
...



“Structured” Arrays

```
# "Data structure" (dtype) that describes the fields and
# type of the items in each array element.
>>> particle_dtype = dtype([('mass','f4'), ('velocity', 'f4')])
# This must be a list of tuples. NumPy doesn't like
# a list of arrays or a tuple of tuples.
>>> particles = array([(1,1), (1,2), (2,1), (1,3)],
                      dtype=particle_dtype)

>>> particles
[(1.0, 1.0) (1.0, 2.0) (2.0, 1.0) (1.0, 3.0)]
# Retrieve the mass for all particles through indexing.
>>> particles['mass']
[ 1.  1.  2.  1.]
```



“Structured” Arrays

```
# Retrieve particle 0 through indexing.
>>> particles[0]
(1, 1)
# Sort particles in place, with velocity as the primary field and
# mass as the secondary field.
>>> particles.sort(order=('velocity', 'mass'))
>>> particles
[(1.0, 1.0) (2.0, 1.0) (1.0, 2.0) (1.0, 3.0)]

# See demo/mutlitype_array/particle.py.
```



Overview

- Available at www.scipy.org
- Open Source BSD Style License
- 34 svn “committers” to the project

CURRENT PACKAGES

- Special Functions ([scipy.special](#))
- Signal Processing ([scipy.signal](#))
- Image Processing ([scipy.ndimage](#))
- Fourier Transforms ([scipy.fftpack](#))
- Optimization ([scipy.optimize](#))
- Numerical Integration ([scipy.integrate](#))
- Linear Algebra ([scipy.linalg](#))
- Input/Output ([scipy.io](#))
- Statistics ([scipy.stats](#))
- Fast Execution ([scipy.weave](#))
- Clustering Algorithms ([scipy.cluster](#))
- Sparse Matrices ([scipy.sparse](#))
- Interpolation ([scipy.interpolate](#))
- More (e.g. [scipy.odr](#), [scipy.maxentropy](#))



Polynomials

- `p = poly1d(<coefficient array>)`
- `p.roots` (`p.r`) are the roots
- `p.coefficients` (`p.c`) are the coefficients
- `p.order` is the order
- `p[n]` is the coefficient of x^n
- `p(val)` evaluates the polynomial at `val`
- `p.integ()` integrates the polynomial
- `p.deriv()` differentiates the polynomial
- Basic numeric operations (+,-,/,*) work
- Acts like `p.c` when used as an array
- Fancy printing

```
>>> p = poly1d([1,-2,4])
>>> print p
      2
x  - 2 x + 4

>>> g = p**3 + p*(3-2*p)
>>> print g
      6      5      4      3      2
x  - 6 x + 25 x - 51 x + 81 x - 58 x +
44

>>> print g.deriv(m=2)
      4      3      2
30 x - 120 x + 300 x - 306 x + 162

>>> print p.integ(m=2,k=[2,1])
      4      3      2
0.08333 x - 0.3333 x + 2 x + 2 x + 1

>>> print p.roots
[ 1.+1.7321j  1.-1.7321j]

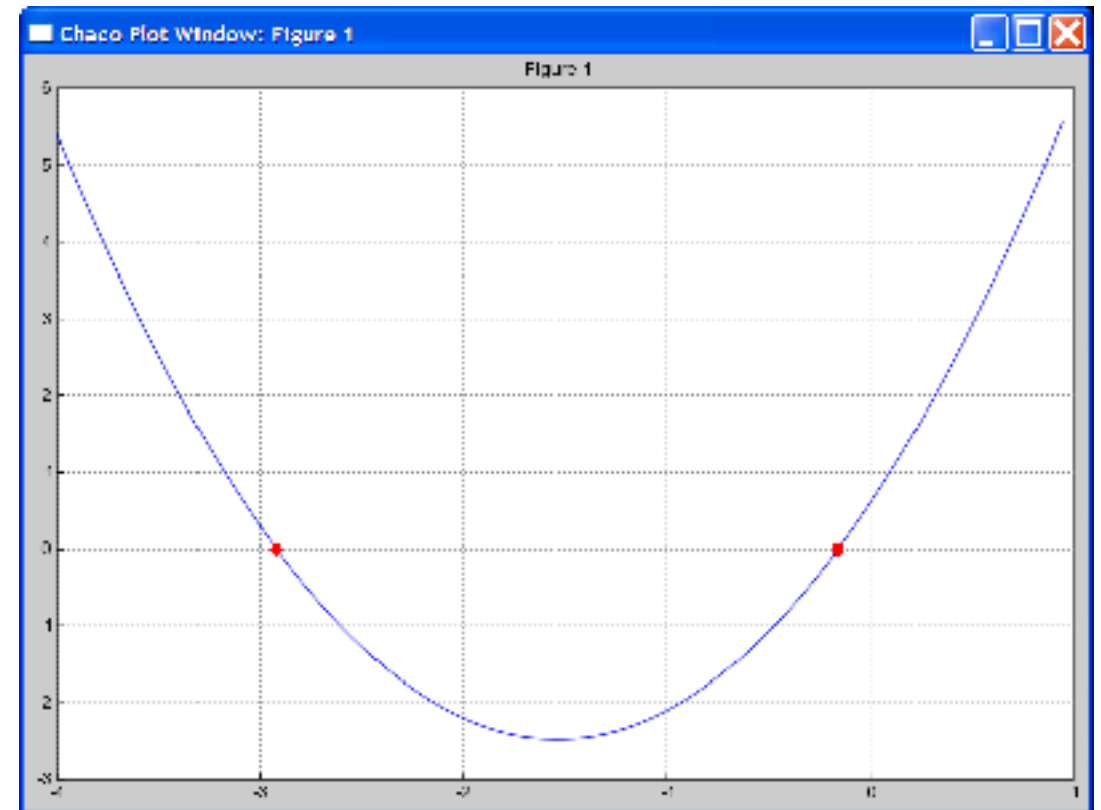
>>> print p.coeffs
[ 1 -2  4]
```



Polynomials

FINDING THE ROOTS OF A POLYNOMIAL

```
>>> p = poly1d([1.3, 4.0, 0.6])
>>> print p
      2
1.3 x + 4 x + 0.6
>>> x = linspace(-4, 1.0, 101)
>>> y = p(x)
>>> plot(x,y,'-')
>>> hold(True)
>>> r = p.roots
>>> s = p(r)
>>> r
array([-0.15812627, -2.9187968 ])
>>> plot(r.real,s.real,'ro')
```





Special Functions

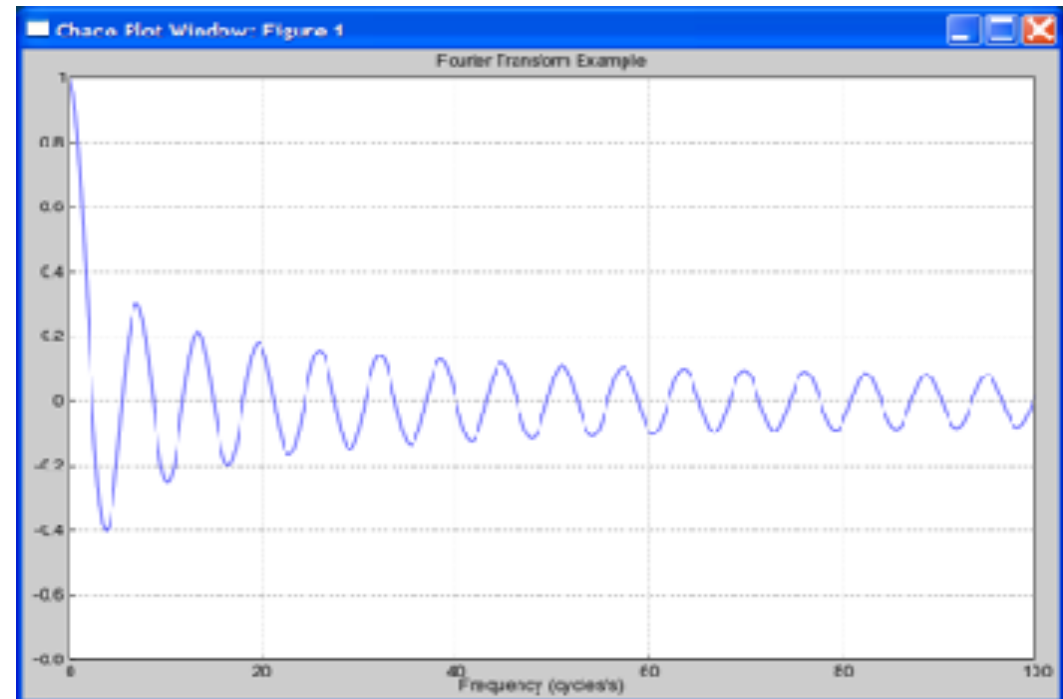
scipy.special

Includes over 200 functions:

Airy, Elliptic, Bessel, Gamma, HyperGeometric, Struve, Error, Orthogonal Polynomials, Parabolic Cylinder, Mathieu, Spheroidal Wave, Kelvin

FIRST ORDER BESSEL EXAMPLE

```
>>> from scipy import special
>>> x = linspace(0, 100, 1001)
>>> j0x = special.j0(x)
>>> plot(x, j0x)
```

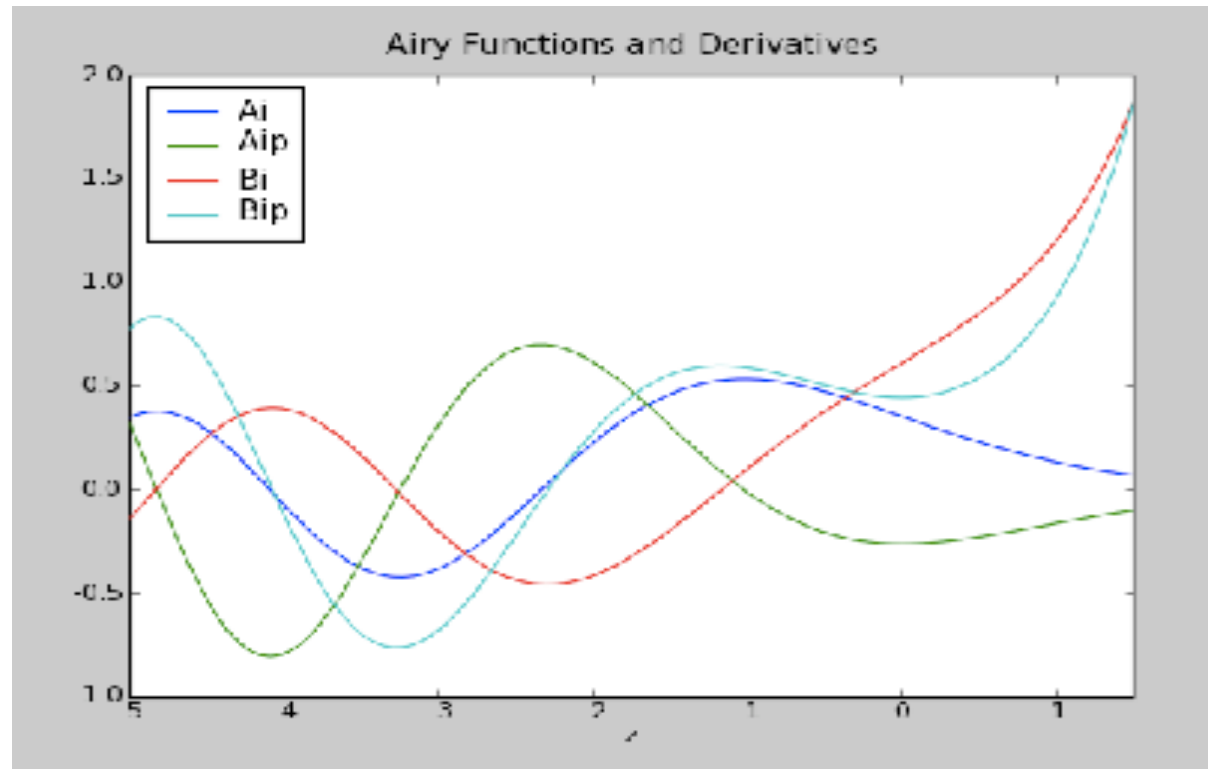




Special Functions

AIRY FUNCTIONS

```
>>> z = linspace(-5, 1.5, 100)
>>> Ai, Aip, Bi, Bip = special.airy(z)
>>> plot(z, array(vals).T)
```





Interpolation

scipy.interpolate --- General purpose Interpolation

•1-d Interpolating Class

- Constructs callable function from data points and desired spline interpolation order.
- Function takes vector of inputs and returns interpolated value using the spline.

•1-d and 2-d spline interpolation (FITPACK)

- Smoothing splines up to order 5
- Parametric splines



1D Spline Interpolation

```
>>> from scipy.interpolate import interp1d
```

```
interp1d(x, y, kind='linear', axis=-1, copy=True, bounds_error=True,  
         fill_value=numpy.nan)
```

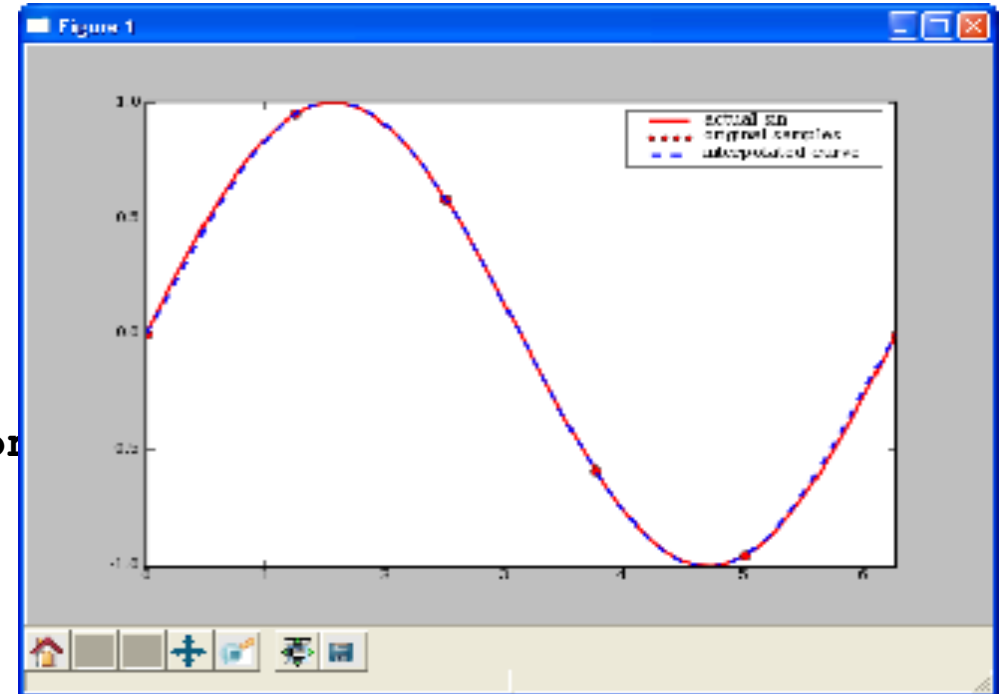
Returns a function that uses interpolation to find the value of new points.

- **x** - 1d array of increasing real values which cannot contain duplicates
- **y** - Nd array of real values whose length along the interpolation axis must be len(x)
- **kind** - kind of interpolation (e.g. 'linear', 'nearest', 'quadratic', 'cubic'). Can also be an integer $n > 1$ which returns interpolating spline (with minimum sum-of-squares discontinuity in n th derivative).
- **axis** - axis of y along which to interpolate
- **copy** - make internal copies of x and y
- **bounds_error** - raise error for out-of-bounds
- **fill_value** - if bounds_error is False, then use this value to fill in out-of-bounds.



1D Spline Interpolation

```
# demo/interpolate/spline.py
from scipy.interpolate import interp1d
from pylab import plot, axis, legend
from numpy import linspace
# sample values
x = linspace(0,2*pi,6)
y = sin(x)
# Create a spline class for interpolation
# kind=5 sets to 5th degree spline.
# kind='nearest' -> zeroth order hold.
# kind='linear' -> linear interpolation
# kind=n -> use an nth order spline
```





1D Spline Interpolation

```
spline_fit = interp1d(x,y,kind=5)
xx = linspace(0,2*pi, 50)
yy = spline_fit(xx)
# display the results.
plot(xx, sin(xx), 'r-', x, y, 'ro', xx, yy, 'b--',
      linewidth=2)
axis('tight')
legend(['actual sin', 'original samples',
       'interpolated curve'])
```



2D Spline Interpolation

```
>>> from scipy.interpolate import interp2d
```

```
interp2d(x, y, z, kind='linear')
```

Returns a function, f , that uses interpolation to find the value of new points: $z_{\text{new}} = f(x_{\text{new}}, y_{\text{new}})$

x - 1d or 2d array

y - 1d or 2d array

z - 1d or 2d array representing function evaluated at x and y

kind - kind of interpolation: 'linear', 'quadratic', or 'cubic'

The shape of x , y , and z must be the same.



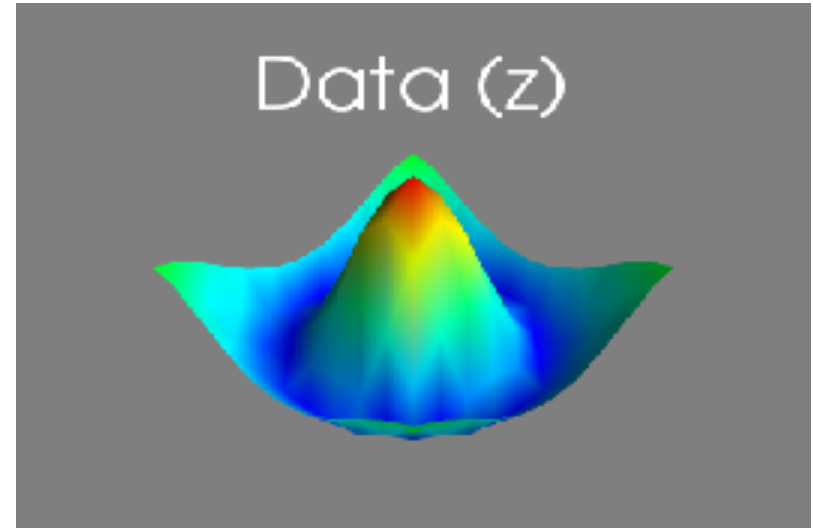
Resulting function is evaluated at cross product of new inputs.



2D Spline Interpolation

EXAMPLE

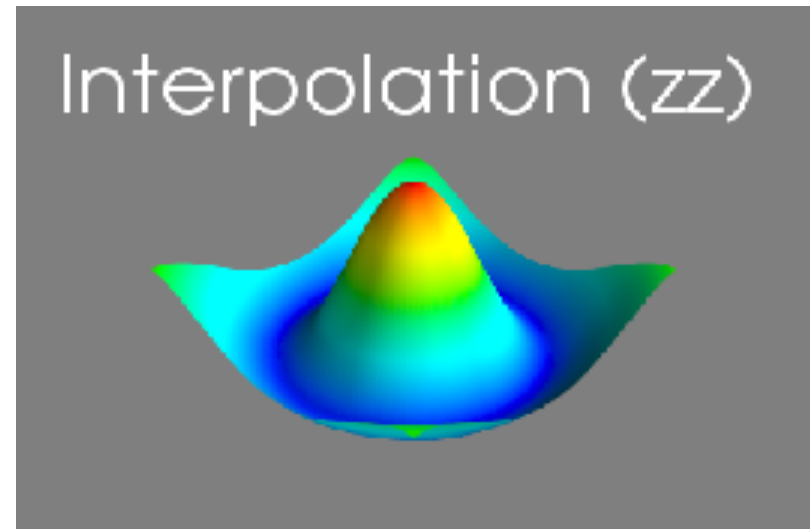
```
>>> from scipy.interpolate import \
...     interp2d
>>> from numpy import hypot, mgrid, \
...     linspace
>>> from scipy.special import j0
>>> x,y = mgrid[-5:6,-5:6]
>>> z = j0(hypot(x,y))
>>> newfunc = interp2d(x, y, z,
...                     kind='cubic')
>>> xx = linspace(-5,5,100)
>>> yy = xx
# xx and yy are 1-d
# result is evaluated on the
# cross product
```





2D Spline Interpolation

```
>>> zz = newfunc(xx,yy)
>>> from enthought.mayavi import mlab
>>> mlab.surf(x,y,z)
>>> x2, y2 = mgrid[-5:5:100j,
...               -5:5:100j]
>>> mlab.surf(x2,y2,zz)
```





Statistics

scipy.stats --- CONTINUOUS DISTRIBUTIONS

over 80
continuous
distributions!

METHODS

pdf entropy

cdf nnlf

rvs moment

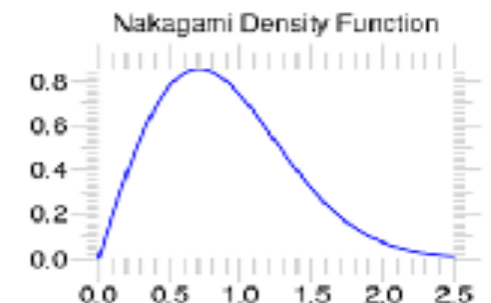
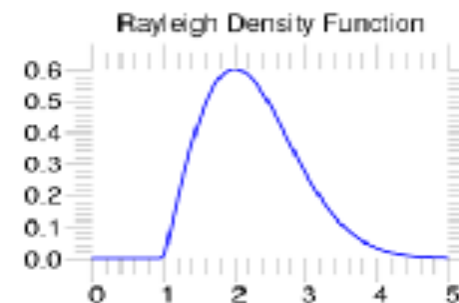
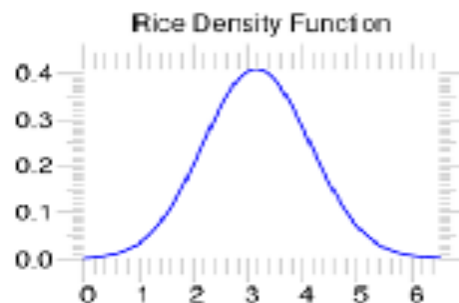
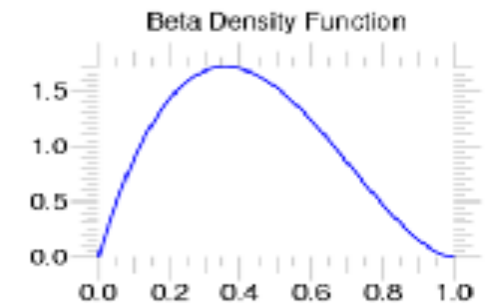
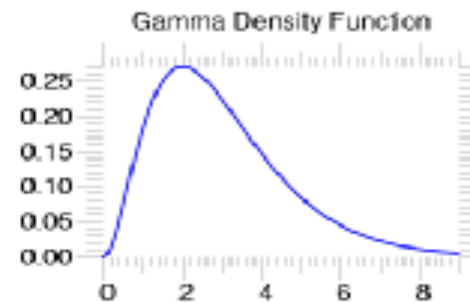
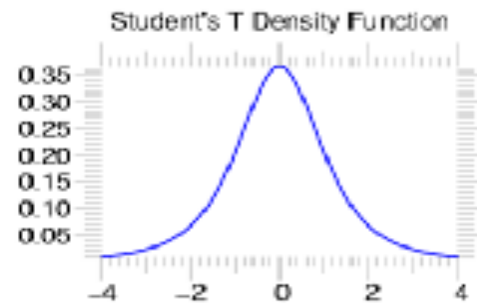
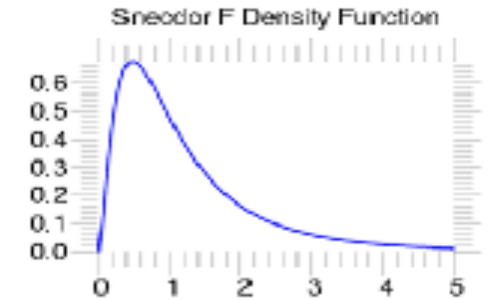
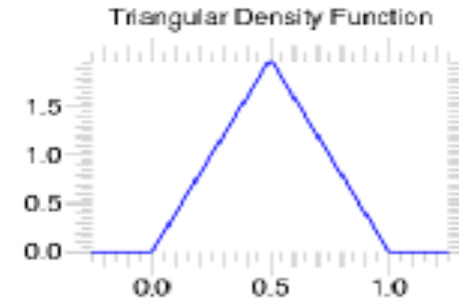
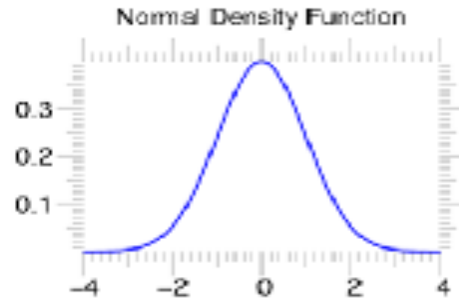
ppf freeze

stats

fit

sf

isf





Statistics

scipy.stats --- Discrete Distributions

10 standard discrete distributions (plus any finite RV)

METHODS

pmf moment

cdf entropy

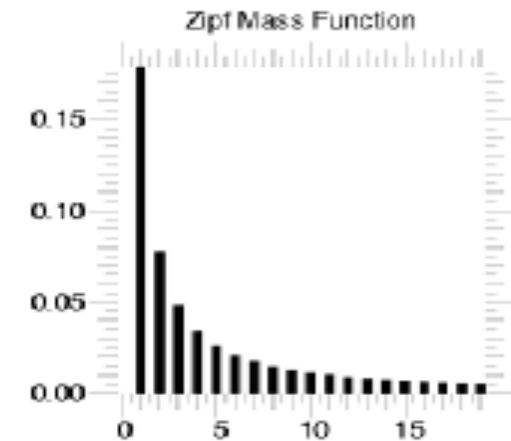
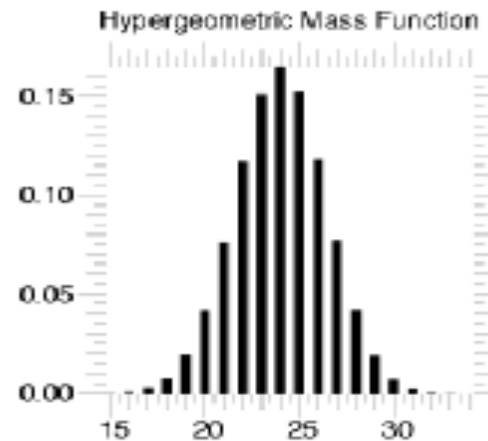
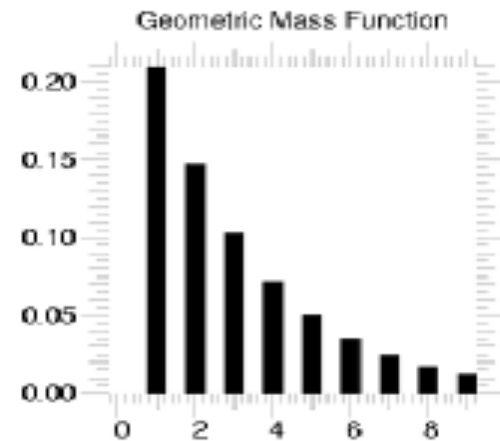
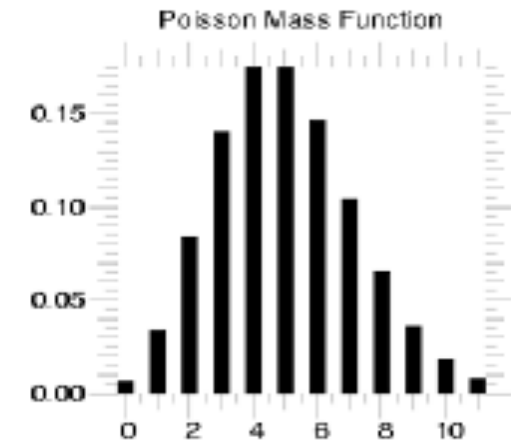
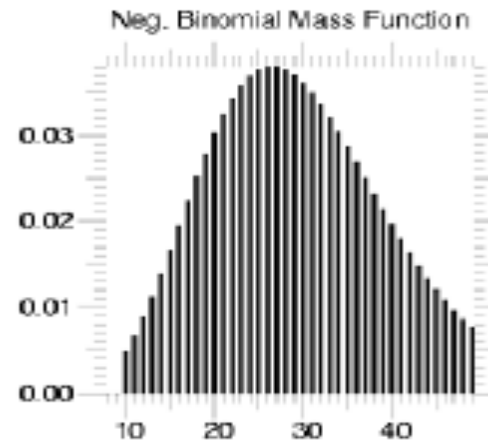
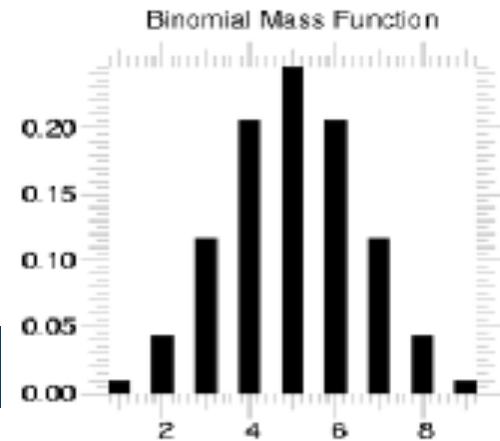
rvs freeze

ppf

stats

sf

isf





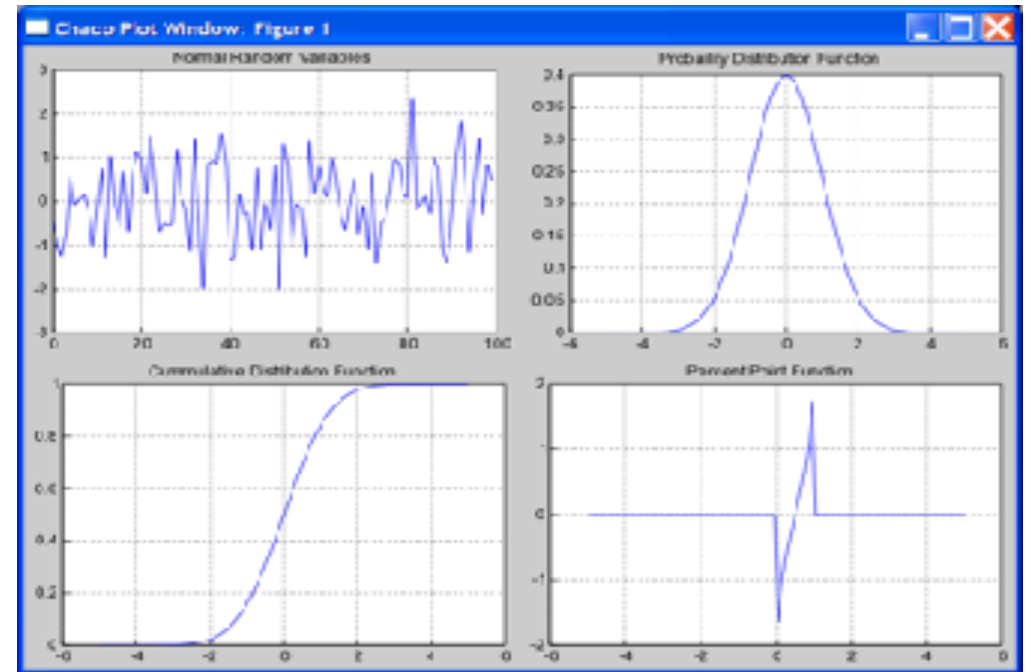
Using stats objects

DISTRIBUTIONS

```
>>> from scipy.stats import norm
# Sample normal dist. 100 times.
>>> samp = norm.rvs(size=100)

>>> x = linspace(-5, 5, 100)
# Calculate probability dist.
>>> pdf = norm.pdf(x)
# Calculate cumulative dist.
>>> cdf = norm.cdf(x)
# Calculate Percent Point Function
>>> ppf = norm.ppf(x)

# Estimate parameters from data
>>> mu, sigma = norm.fit(samp)
>>> print "%4.2f, %4.2f" % (mu, sigma)
-0.14, 1.01
```





Using stats objects

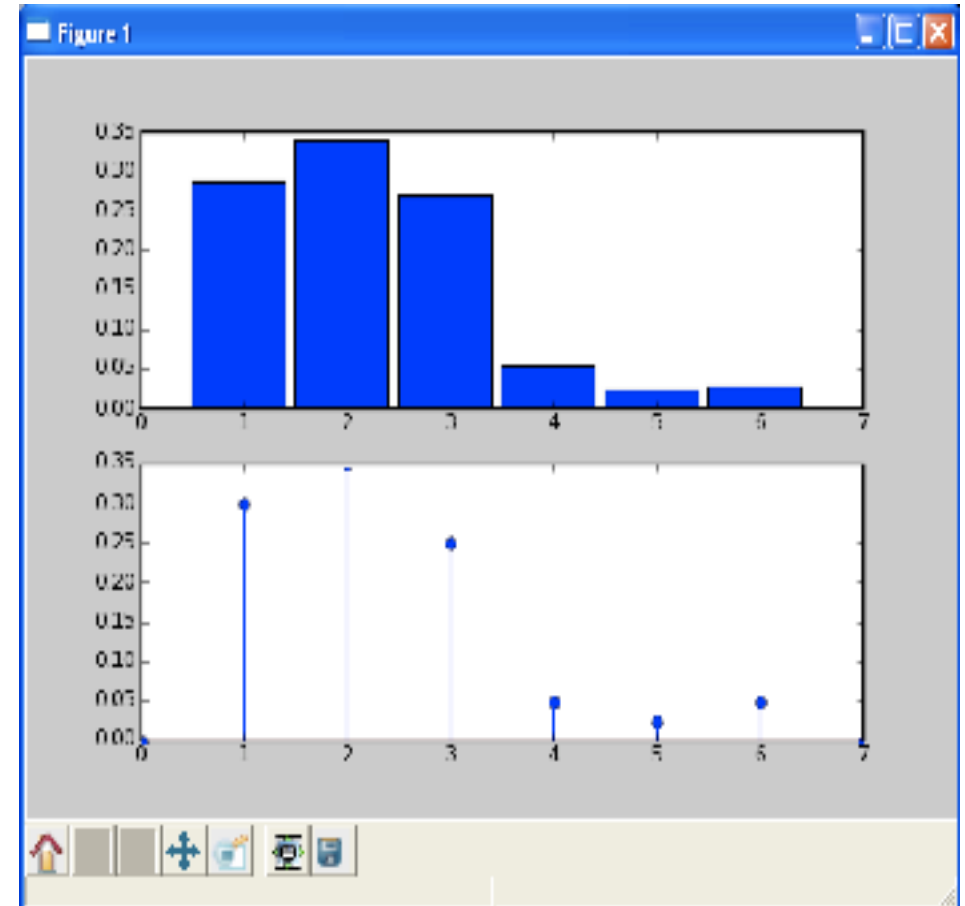
CREATING NEW DISCRETE DISTRIBUTIONS

```
# Create loaded dice.
>>> from scipy.stats import rv_discrete
>>> xk = [1,2,3,4,5,6]
>>> pk = [0.3,0.35,0.25,0.05,
          0.025,0.025]

>>> new = rv_discrete(name='loaded',
                      values=(xk,pk))

# Calculate histogram
>>> samples = new.rvs(size=1000)
>>> bins=linspace(0.5,5.5,6)
>>> subplot(211)
>>> hist(samples,bins=bins,normed=True)

# Calculate pmf
>>> x = range(0,8)
>>> subplot(212)
>>> stem(x,new.pmf(x))
```



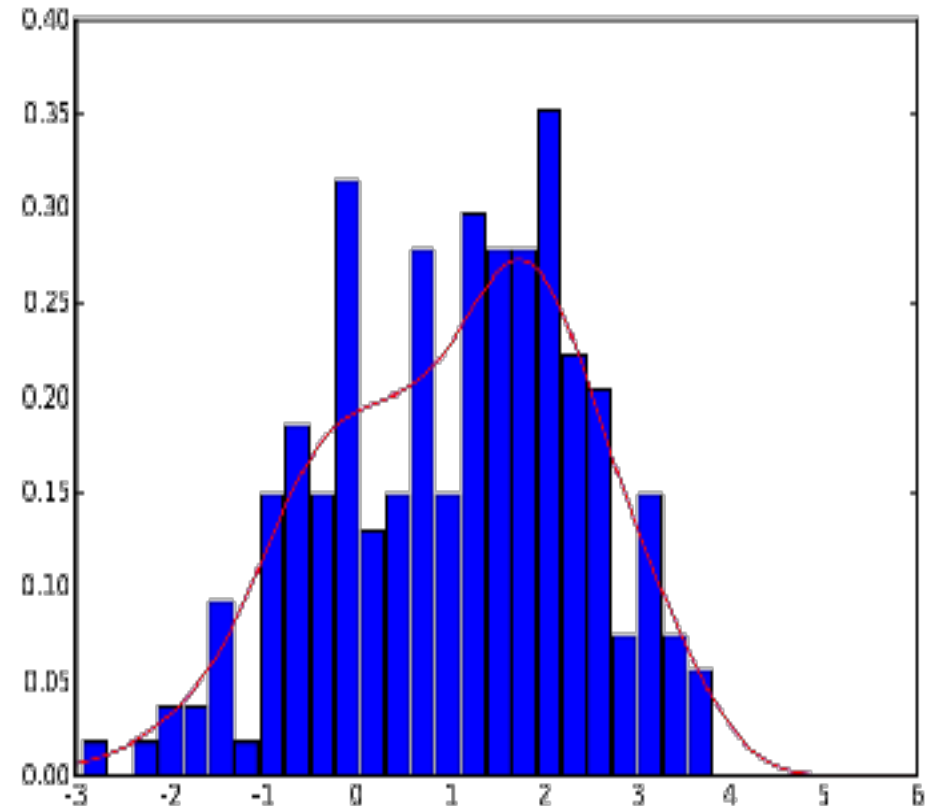


Statistics

CONTINUOUS DISTRIBUTION ESTIMATION USING GAUSSIAN KERNELS

```
# Sample two normal distributions
# and create a bi-modal distribution
>>> rv1 = stats.norm()
>>> rv2 = stats.norm(2.0,0.8)
>>> samples = hstack([rv1.rvs(size=100),
                      rv2.rvs(size=100)])

# Use a gaussian kernel density to
# estimate the pdf for the samples.
>>> from scipy.stats.kde import
    gaussian_kde
>>> approximate_pdf =
    gaussian_kde(samples)
>>> x = linspace(-3,6,200)
# Compare the histogram of the samples to
# the pdf approximation.
>>> hist(samples, bins=25, normed=True)
>>> plot(x, approximate_pdf(x), 'r')
```





Linear Algebra

scipy.linalg --- FAST LINEAR ALGEBRA

- Uses ATLAS if available --- very fast
- Low-level access to BLAS and LAPACK routines in modules `linalg.fblas`, and `linalg.flapack` (FORTRAN order)
- High level matrix routines
 - Linear Algebra Basics: `inv`, `solve`, `det`, `norm`, `lstsq`, `pinv`
 - Decompositions: `eig`, `lu`, `svd`, `orth`, `cholesky`, `qr`, `schur`
 - Matrix Functions: `expm`, `logm`, `sqrtm`, `cosm`, `coshm`, `funm` (general matrix functions)



Linear Algebra

LU FACTORIZATION

```
>>> from scipy import linalg
>>> a = array([[1,3,5],
...           [2,5,1],
...           [2,3,6]])
# time consuming factorization
>>> lu, piv = linalg.lu_factor(a)

# fast solve for 1 or more
# right hand sides.
>>> b = array([10,8,3])
>>> linalg.lu_solve((lu, piv), b)
array([-7.82608696,  4.56521739,
        0.82608696])
```

EIGEN VALUES AND VECTORS

```
>>> from scipy import linalg
>>> a = array([[1,3,5],
...           [2,5,1],
...           [2,3,6]])
# compute eigen values/vectors
>>> vals, vecs = linalg.eig(a)
# print eigen values
>>> vals
array([ 9.39895873+0.j,
       -0.73379338+0.j,
        3.33483465+0.j])
# eigen vectors are in columns
# print first eigen vector
>>> vecs[:,0]
array([-0.57028326,
       -0.41979215,
       -0.70608183])
# norm of vector should be 1.0
>>> linalg.norm(vecs[:,0])
1.0
```




Matrix Objects

STRING CONSTRUCTION

```
>>> from numpy import mat
>>> a = mat('[1,3,5;2,5,1;2,3,6]')
>>> a
matrix([[1, 3, 5],
        [2, 5, 1],
        [2, 3, 6]])
```

TRANPOSE ATTRIBUTE

```
>>> a.T
matrix([[1, 2, 2],
        [3, 5, 3],
        [5, 1, 6]])
```

INVERTED ATTRIBUTE

```
>>> a.I
matrix([[ -1.1739,  0.1304,  0.956],
        [ 0.4347,  0.1739, -0.391],
        [ 0.1739, -0.130,  0.0434]
        ])
```

note: reformatted to fit slide

DIAGONAL

```
>>> a.diagonal()
matrix([[1, 5, 6]])
>>> a.diagonal(-1)
matrix([[3, 1]])
```

SOLVE

```
>>> b = mat('10;8;3')
>>> a.I*b
matrix([[ -7.82608696],
        [ 4.56521739],
        [ 0.82608696]])
```

```
>>> from scipy import linalg
>>> linalg.solve(a,b)
matrix([[ -7.82608696],
        [ 4.56521739],
        [ 0.82608696]])
```



Optimization

scipy.optimize --- unconstrained minimization and root finding

- **Unconstrained Optimization**

`fmin` (Nelder-Mead simplex), `fmin_powell` (Powell's method), `fmin_bfgs` (BFGS quasi-Newton method), `fmin_ncg` (Newton conjugate gradient), `leastsq` (Levenberg-Marquardt), `anneal` (simulated annealing global minimizer), `brute` (brute force global minimizer), `brent` (excellent 1-D minimizer), `golden`, `bracket`

- **Constrained Optimization**

`fmin_l_bfgs_b`, `fmin_tnc` (truncated newton code), `fmin_cobyla` (constrained optimization by linear approximation), `fminbound` (interval constrained 1-d minimizer)

- **Root finding**

`fsolve` (using MINPACK), `brentq`, `brenth`, `ridder`, `newton`, `bisect`, `fixed_point` (fixed point equation solver)

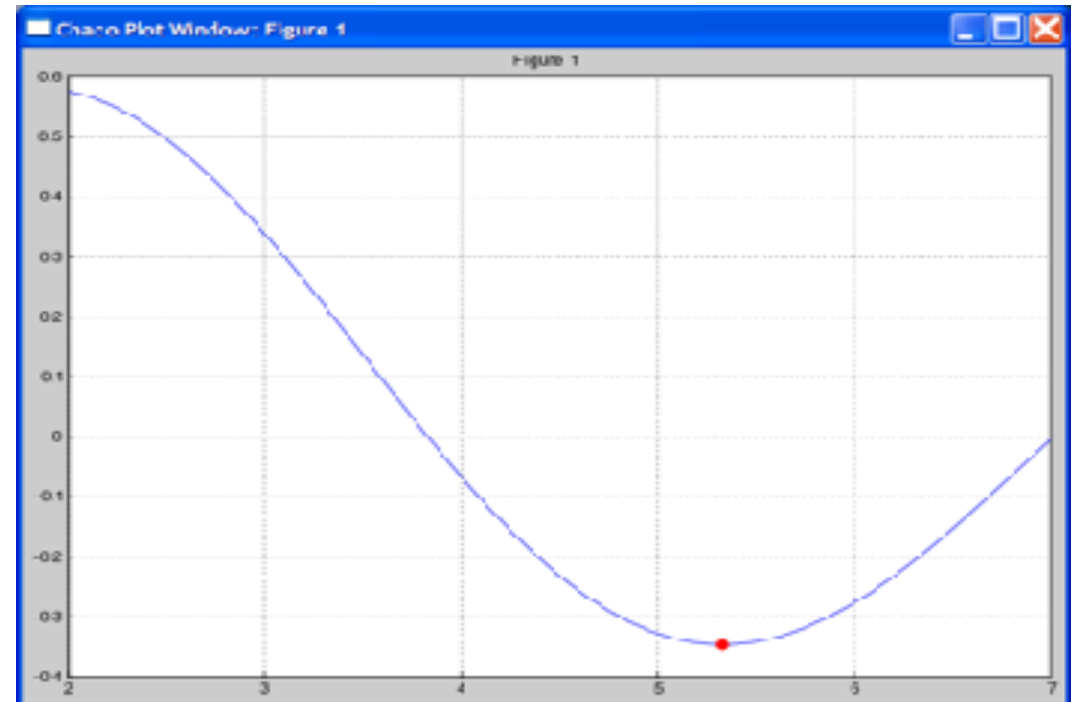


Optimization: 1D Minimization

EXAMPLE: MINIMIZE BESSEL FUNCTION

```
# minimize 1st order bessel
# function between 4 and 7
>>> from scipy.special import j1
>>> from scipy.optimize import \
...     fminbound

>>> x = r_[2:7.1:.1]
>>> j1x = j1(x)
>>> plot(x,j1x,'-')
>>> hold(True)
>>> x_min = fminbound(j1,4,7)
>>> j1_min = j1(x_min)
>>> plot([x_min],[j1_min],'ro')
```





Optimization: Solving Nonlinear Equations

FSOLVE

```
>>> def equations(x,a,b,c):  
...     x0, x1, x2 = x  
...     eqs = \  
...     [3 * x0 - cos(x1*x2) + a,  
...     x0**2 - 81*(x1+0.1)**2 + sin(x2) + b,  
...     exp(-x0*x1) + 20*x2 + c]  
...     return eqs
```

```
# coefficients
```

```
>>> a = -0.5
```

```
>>> b = 1.06
```

```
>>> c = (10 * pi - 3.0) / 3
```

```
# Optimization start location.
```

```
>>> initial_guess = [0.1, 0.1, -0.1]
```

```
# Solve the system of non-linear equations.
```

```
>>> root = optimize.fsolve(equations, initial_guess, args=(a, b, c))
```

```
>>> print root
```

```
root: [ 5.00e-01  1.38e-13 -5.24e-01]
```

```
>>> print nonlin(root, a, b, c)
```

```
solution at root: [0.0, -2.2311...e-012, 7.46069...e-014]
```

SYSTEM OF EQUATIONS

$$3x_0 - \cos(x_1x_2) + a = 0$$

$$x_0^2 - 81(x_1 + 0.1)^2 + \sin(x_2) + b = 0$$

$$e^{-x_0x_1} + 20x_2 + c = 0$$



Optimization: Using Derivatives

FMIN: WITHOUT DERIVATIVE

```
>>> from scipy.optimize import rosen, fmin
>>> initial_guess = [1.3, 0.7, 0.8, 1.9, 1.2]
>>> optimal = optimize.fmin(rosen, x0, xtol=1e-7)
```

Optimization terminated successfully.

Current function value: 0.000000

Iterations: 234

Function evaluations: 387

```
>>> print optimal
```

```
optimal: [ 1.  1.  1.  1.  1.]
```

Rosenbrock function

$$f(\mathbf{x}) = \sum_{i=1}^{N-1} 100 \left(x_i - x_{i-1}^2 \right)^2 + (1 - x_{i-1})^2.$$



Optimization: Using Derivatives

FMIN_BFGS: USING DERIVATIVE

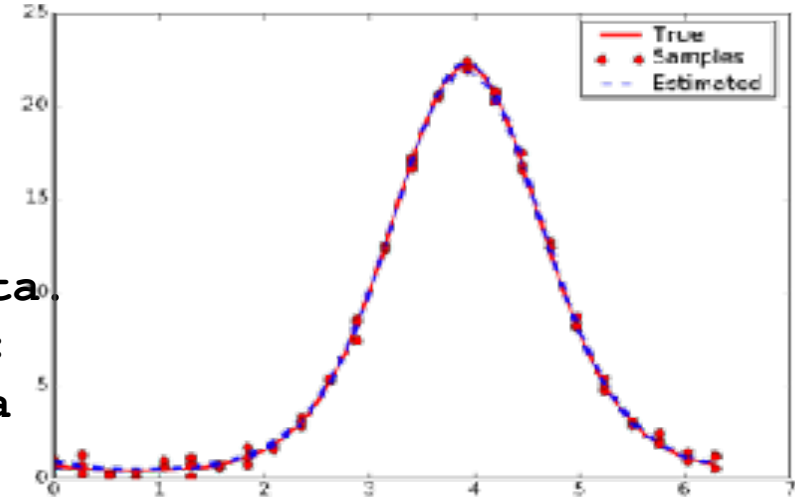
```
>>> from scipy.optimize import rosen_der, fmin_bfgs
>>> optimal = fmin_bfgs(rosen, initial_guess, fprime=rosen_der)
Optimization terminated successfully.
Current function value: 0.000000
Iterations: 51
Function evaluations: 63
Gradient evaluations: 63
>>> print optimal
optimal: [ 1.  1.  1.  1.  1.]
```



Optimization: Data Fitting

NONLINEAR LEAST SQUARES

```
>>> from scipy.optimize import leastsq
# Define the function to fit.
>>> def function(x, a , b, f, phi):
...     result = a * exp(-b * sin(f * x + phi))
...     return result
# And an error function that compares it to data.
>>> def error_function(params, x_data, y_data):
...     result = func(x_data, *params) - y_data
...     return result
# Create a noisy data set.
>>> actual_params = [3, 2, 1, pi/4]
>>> x = linspace(0,2*pi,25)
>>> exact = function(x, *actual_params)
>>> noisy = exact + 0.3 * randn(len(x))
```





Optimization: Data Fitting

```
# Use least squares to to estimate the function parameters from the
noisy data.

>>> initial_guess = [1,1,1,1]

>>> estimated_params, d = leastsq(error_function, initial_guess,
    args=(x, noisy))

>>> estimated_params
array([3.1705, 1.9501, 1.0206, 0.7034])
```



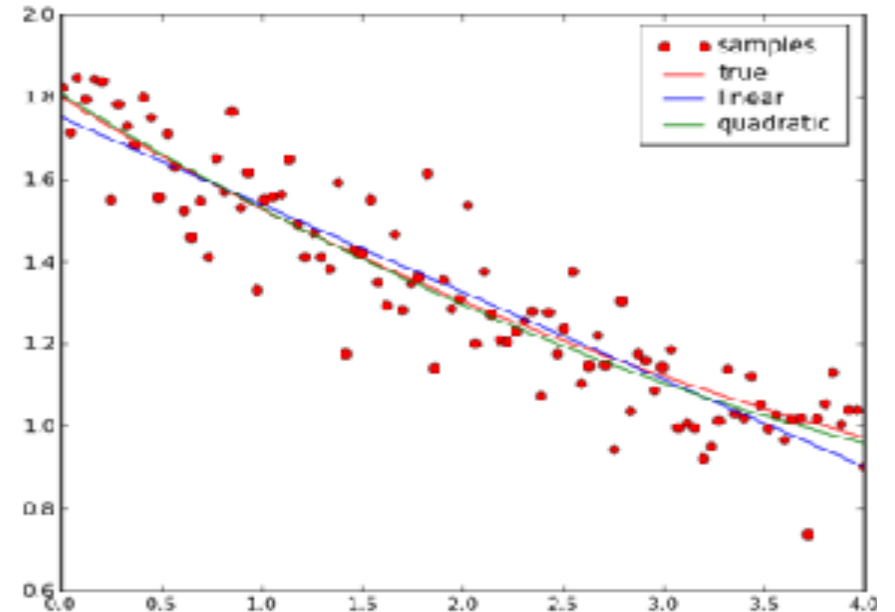

Fitting Polynomials (NumPy)

POLYFIT(X, Y, DEGREE)

```
>>> from numpy import polyfit, poly1d
>>> from scipy.stats import norm
# Create clean data.
>>> x = linspace(0, 4.0, 100)
>>> y = 1.5 * exp(-0.2 * x) + 0.3
# Add a bit of noise.
>>> noise = 0.1 * norm.rvs(size=100)
>>> noisy_y = y + noise

# Fit noisy data with a linear model.
>>> linear_coef = polyfit(x, noisy_y, 1)
>>> linear_poly = poly1d(linear_coef)
>>> linear_y = linear_poly(x),

# Fit noisy data with a quadratic model.
>>> quad_coef = polyfit(x, noisy_y, 2)
>>> quad_poly = poly1d(quad_coef)
>>> quad_y = quad_poly(x)
```





Signal Processing

scipy.signal --- Signal and Image Processing

What's Available?

Filtering

General 2-D Convolution (more boundary conditions)

N-D convolution

B-spline filtering

N-D Order filter, N-D median filter, faster 2d version,

IIR and FIR filtering and filter design

LTI systems

System simulation

Impulse and step responses

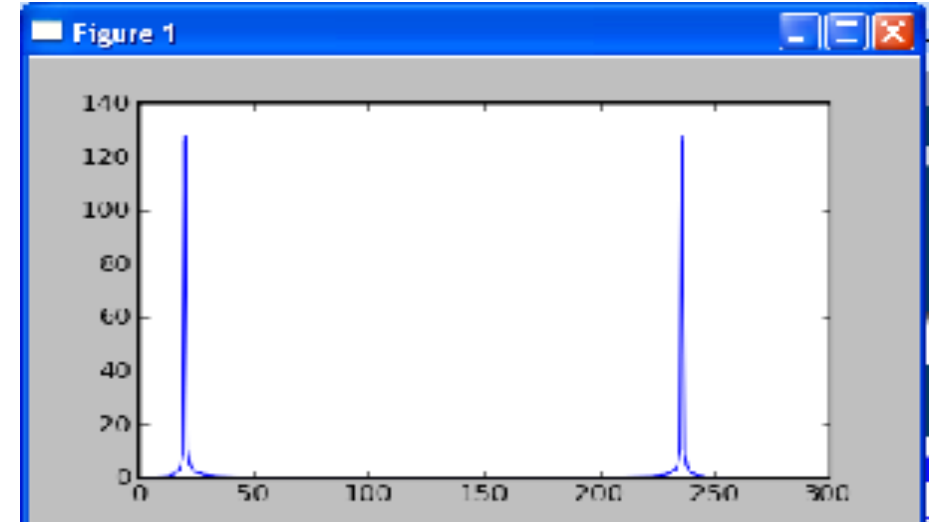
Partial fraction expansion



FFT Functions

FFT

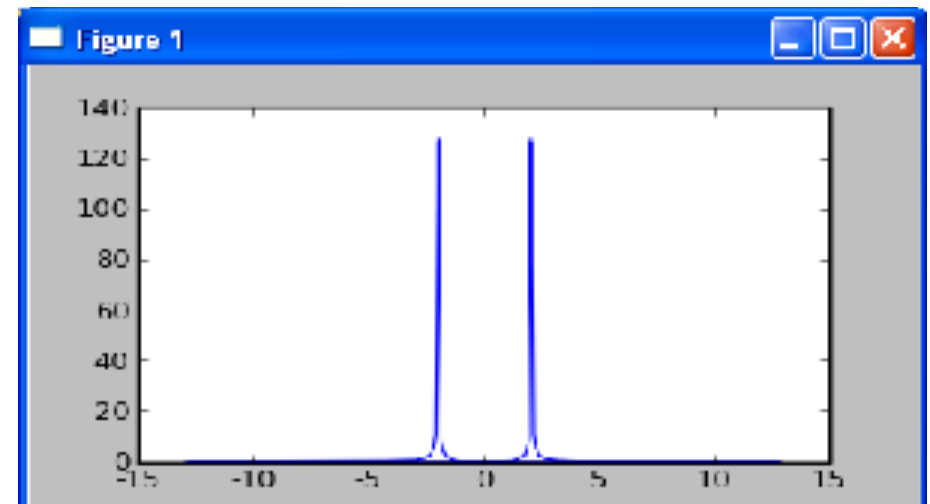
```
# Fast Fourier Transform
>>> from scipy.fftpack import *
>>> f = 2 # Hz
>>> w = 2*pi * f
>>> t = linspace(0,10,256)
>>> s = sin(w*t)
>>> S = fft(s)
>>> plot(abs(S))
```



FFTFREQ

```
# Frequencies in Hz for
# fft samples.

# Sampling rate
>>> rate = 10/256.
>>> f = fftfreq(256, rate)
>>> plot(f,abs(S))
```



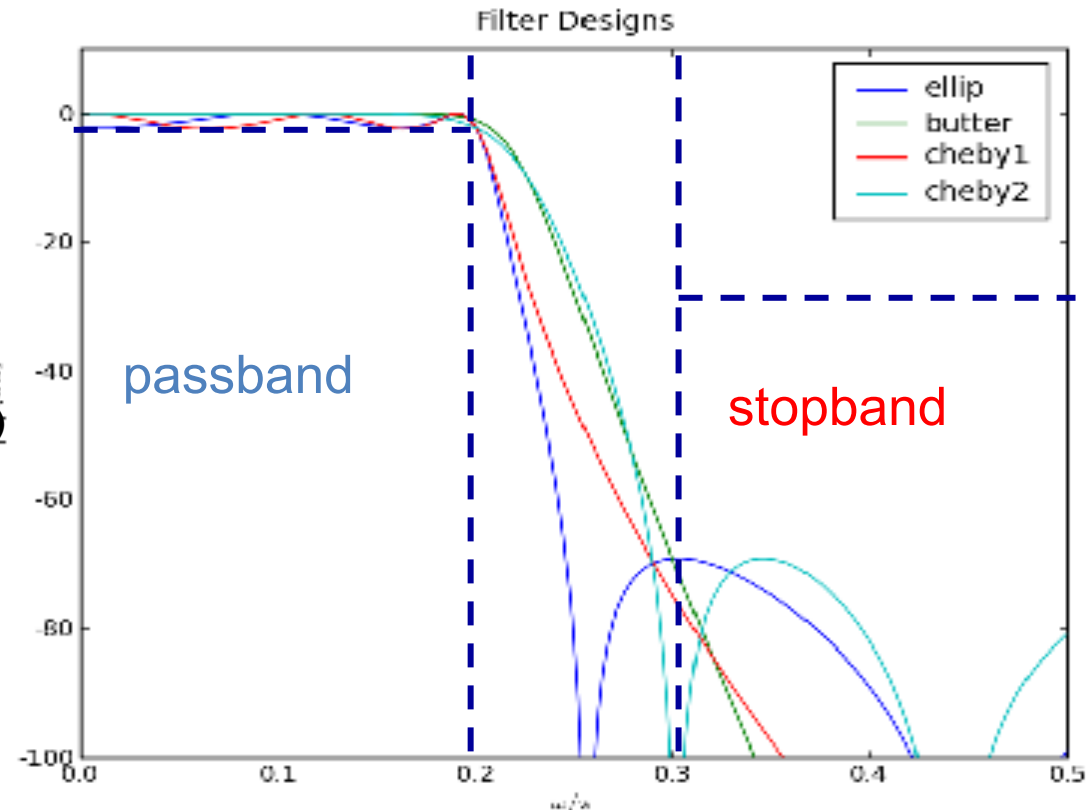


Filter Design

```
iirdesign(pass_edges, stop_edges, maximum_loss_in_passband,  
         minimum_attenuation_in_stopband, ftype=type_of_filter)
```

IIR FILTER DESIGN

```
# Infinite Impulse Response  
# filter design  
>>> import scipy.signal as ss  
>>> for ftype in ['ellip', 'butter',  
...             'cheby1', 'cheby2']:  
...     b,a = ss.iirdesign(0.2, 0.3,  
...                     1, 30,  
...                     ftype=ftype)  
...     w,h = ss.freqz(b, a)  
...     plot(w/pi, 20*log(abs(h)),  
...         label=ftype)  
>>> xlabel(r'$\omega/\pi$')  
>>> ylabel('|H| (dB)')  
>>> title('Filter Designs')  
>>> legend()
```





LTI Systems

```
>>> b,a = [1],[1,6,25]
>>> ltisys = signal.lti(b,a)
>>> t,h = ltisys.impulse()
>>> ts,s = ltisys.step()
>>> plot(t,h,ts,s)
>>> legend(['Impulse response','Step response'])
```

$$H(s) = \frac{1}{s^2 + 6s + 25}$$

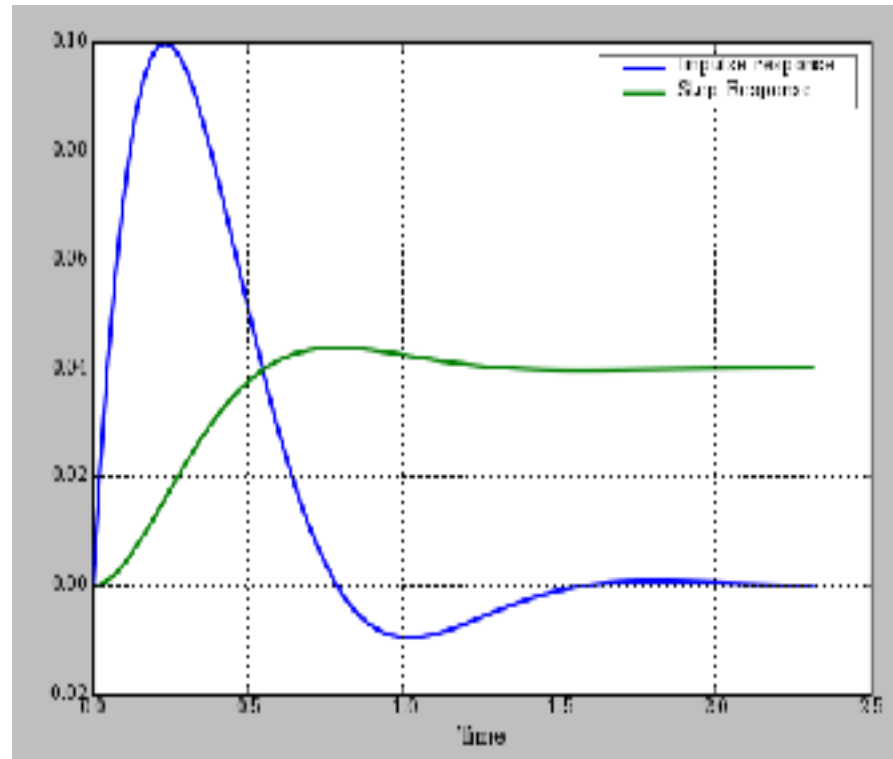
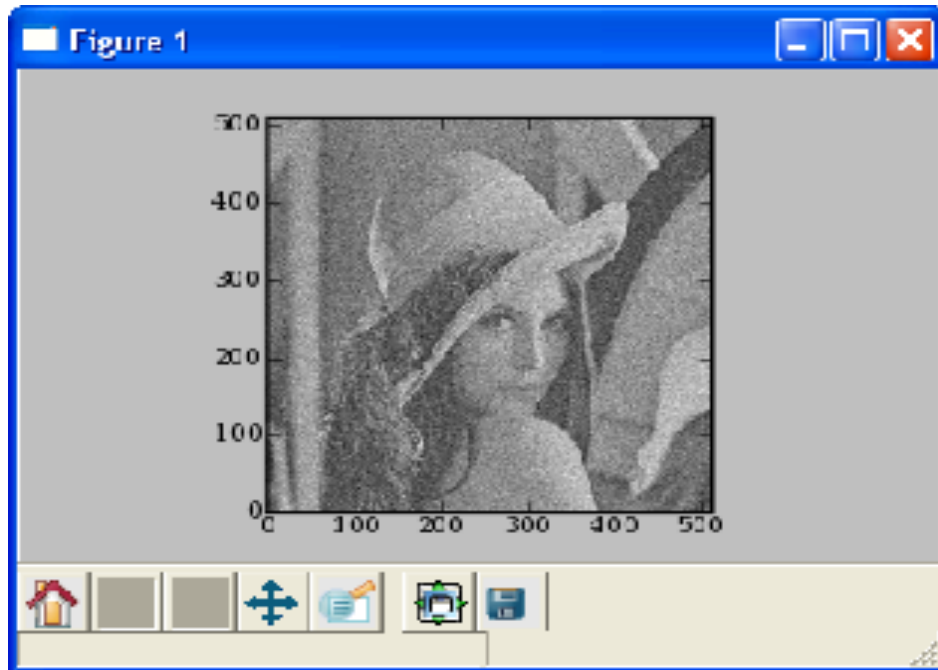




Image Processing

```
# Noise removal using wiener filter
>>> from scipy.stats import norm
>>> ln = lena + norm(0,32).rvs(lena.shape)
>>> imshow(ln)
>>> cleaned = signal.wiener(ln)
>>> imshow(cleaned)
```

NOISY IMAGE



FILTERED IMAGE

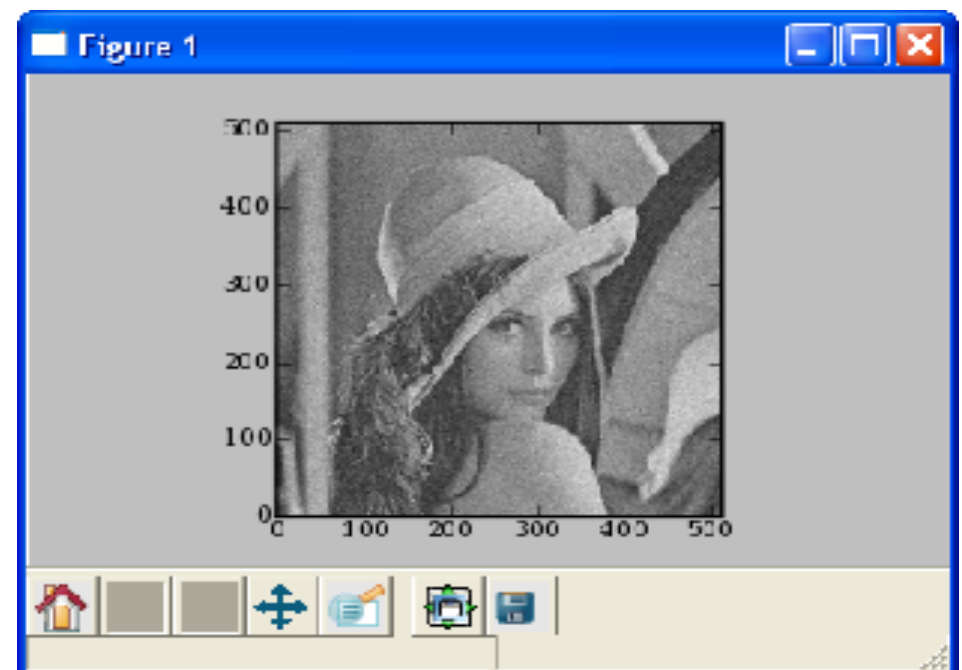
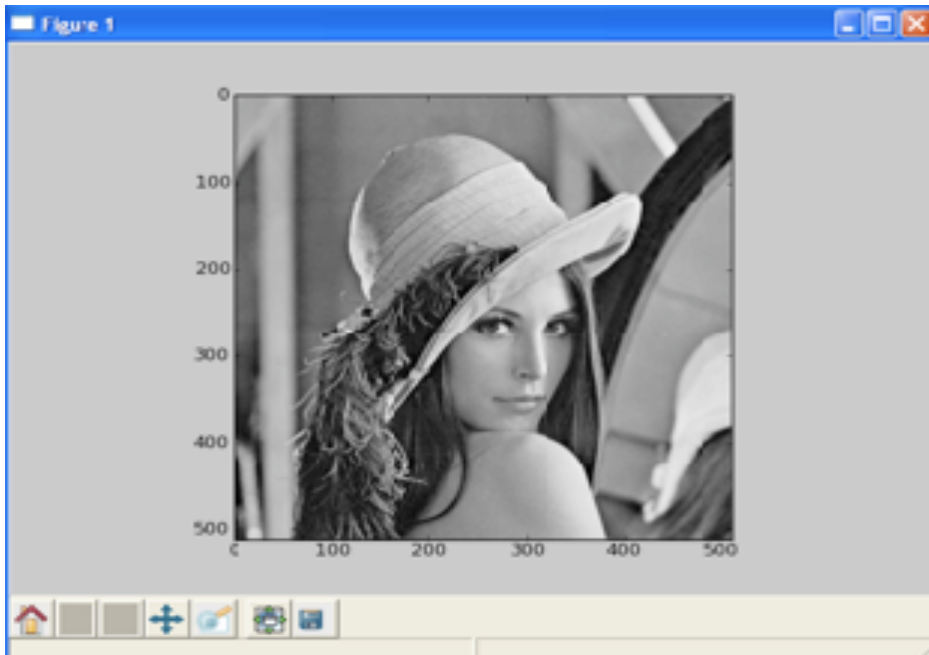




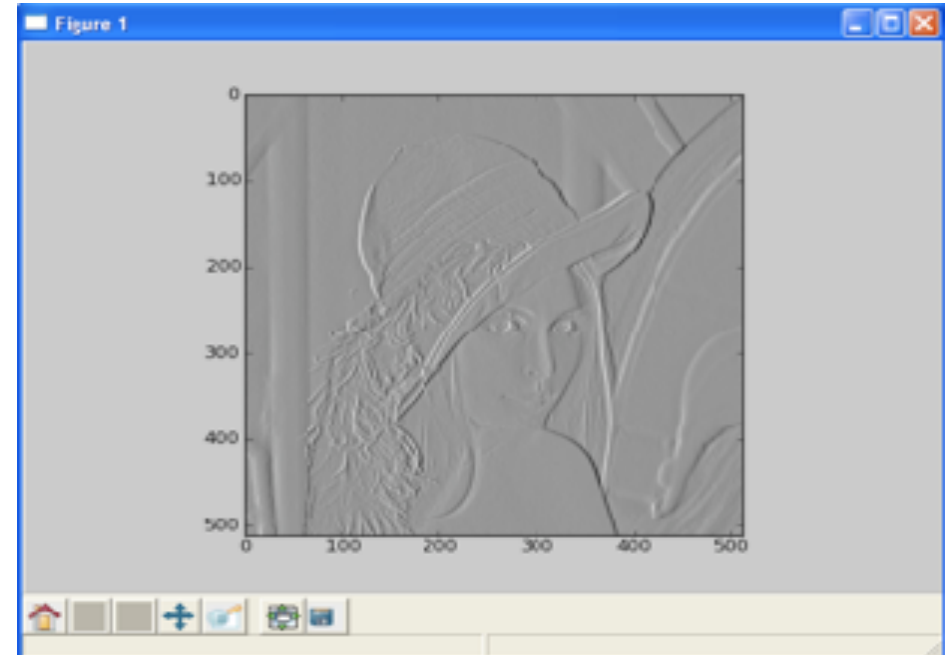
Image Processing

```
# Edge detection using Sobel filter  
>>> from scipy.ndimage.filters import sobel  
>>> imshow(lena)  
>>> edges = sobel(lena)  
>>> imshow(edges)
```

NOISY IMAGE



FILTERED IMAGE





Integration

scipy.integrate --- General purpose Integration

- **Ordinary Differential Equations (ODE)**

`integrate.odeint`, `integrate.ode`

- **Samples of a 1-d function**

`integrate.trapz` (trapezoidal Method), `integrate.simps` (Simpson Method), `integrate.romb` (Romberg Method)

- **Arbitrary callable function**

`integrate.quad` (general purpose), `integrate.dblquad` (double integration), `integrate.tplquad` (triple integration),
`integrate.fixed_quad` (fixed order Gaussian integration),
`integrate.quadrature` (Gaussian quadrature to tolerance),
`integrate.romberg` (Romberg)



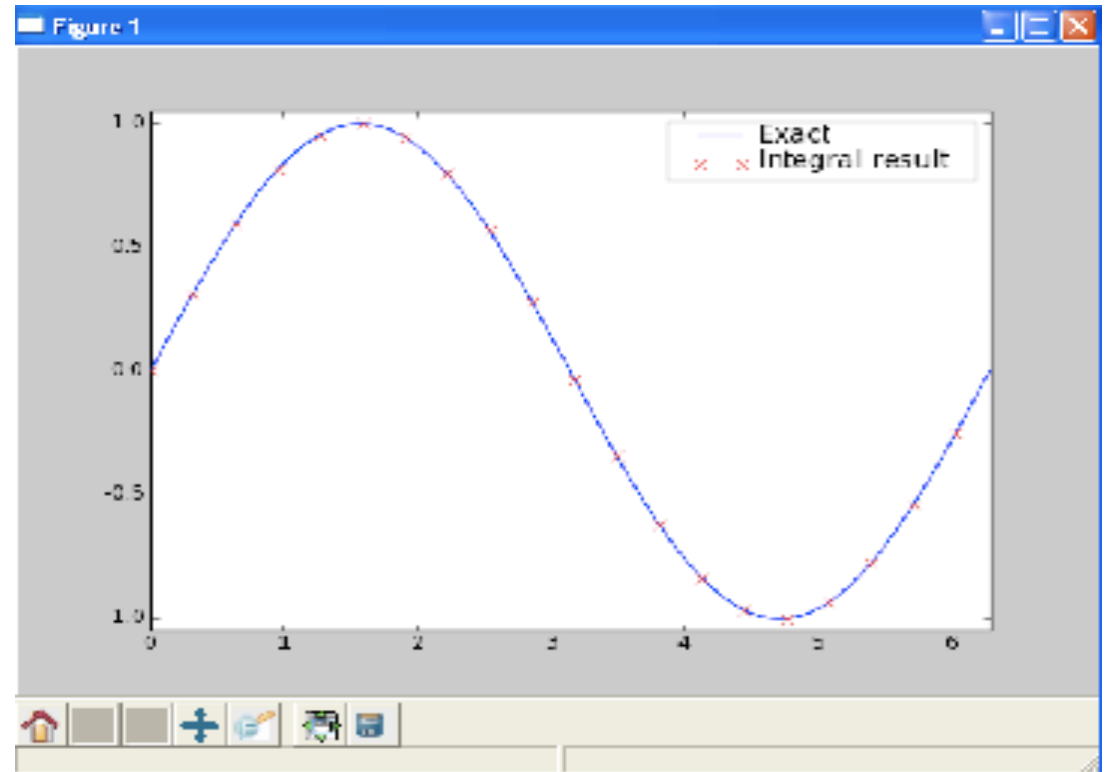
Integration

EXAMPLE (INTEGRATE A CALLABLE)

```
# Compare sin to integral(cos)
>>> def func(x):
    return integrate.quad(cos, 0, x)

[0]
>>> vecfunc = vectorize(func)

>>> x = r_[0:2*pi:100j]
>>> x2 = x[::5]
>>> y = sin(x)
>>> y2 = vecfunc(x2)
>>> plot(x, y, x2, y2, 'rx')
>>> legend(['Exact',
...        'Integral Result'])
```

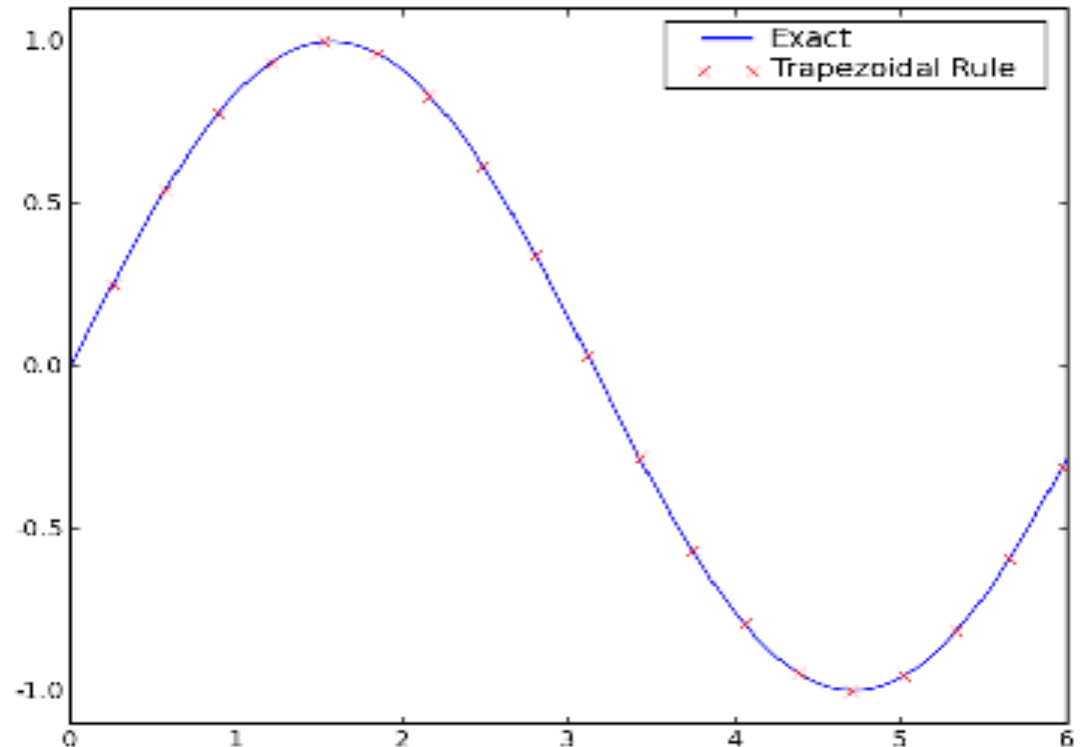




Integration

EXAMPLE (INTEGRATE FROM SAMPLES)

```
# Compare sin to integral(cos)
>>> x = r_[0:2*pi:100j]
>>> y = sin(x)
>>> fx = cos(x)
>>> N = len(x)+1
>>> y2 = [trapz(fx[:i],x[:i])
...       for i in range(5,N,5)]
>>> x2 = x[4::5]
>>> plot(x,y,x2,y2,'rx')
>>> legend(['Exact',
...        'Trapezoidal Rule'])
```





Ordinary Differential Equation

```
>>> from scipy.integrate import odeint
```

Find $y(t)$ given $y(t_0)$ and

$$\frac{dy}{dt} = f(y, t)$$

```
odeint(func, y0, t, args=())
```

`func` - `func(y,tn,...)` calculates dy/dt at `tn`, `y` can be a vector; `func` should then return the same length vector

`y0` - initial value of `y` (can be a vector)

`t` - a sequence of time points at which to solve for `y`, the initial value, `t0`, should be the first element of the sequence

`args` - any extra arguments needed by `func`



MATLAB FILES

SAVE FILE

```
>>> from scipy.io import mio
>>> mio.savemat('tst.mat',
               {'x': 1,
                'y': 2})
```

LOAD MATLAB 7.1 OR BEFORE

```
>>> mf = mio.loadmat('tst.mat')
>>> print mf['x']
1
>>> print mf['y']
2
```

LOAD - MATLAB 7.3 OR AFTER

```
# Matlab 7.3 uses HDF files
# by default. The 'tables'
# library handles hdf files
# well.
>>> import tables
>>> f = tables.openFile('tst.mat')
>>> x = file.root.x[:]
>>> print x
1
>>> y = file.root.y[:]
>>> print y
2
```



GA and Clustering

scipy.sandbox.ga --- Basic Genetic Algorithm Optimization

Routines and classes to simplify setting up a genome and running a genetic algorithm evolution

scipy.cluster --- Basic Clustering Algorithms

- **Observation whitening**
- **Vector quantization**
- **K-means algorithm**

`cluster.vq.whiten`

`cluster.vq.vq`

`cluster.vq.kmeans`



Enthought Tool Suite

TRAITS

Initialization, Validation, Observation, and Visualization of Python class attributes

KIVA

2D primitives supporting path based rendering, affine transforms, alpha blending and more.

ENABLE

Object based 2D drawing canvas

CHACO

Plotting toolkit for building complex, interactive 2D plots

MAYAVI

3D Visualization of Scientific Data based on VTK

ENVISAGE

Application plugin framework for building scriptable and extensible applications



What are traits?

Traits provide additional characteristics for Python object attributes:

- Notification
- Visualization
- Others
 - Validation
 - Initialization
 - Delegation



Defining Simple Traits

```
from enthought.traits.api import HasTraits, Float
```

```
class Rectangle(HasTraits): # <----- Derive from HasTraits
    """ Simple rectangle class with two traits.
    """
    # Width of the rectangle
    width = Float # <----- Declare Traits

    # Height of the rectangle
    height = Float # <----- Declare Traits
```

```
# Demo Code
```

```
>>> rect = Rectangle()
>>> rect.width
0.0
```

```
# Set rect width to 1.0
```

```
>>> rect.width = 1.0
1.0
```

Note: Run `main()` for this example to execute similar commands to those below.

```
In[1]: run rect_1.py
In[2]: main()
```

```
# Float traits convert integers
```

```
>>> rect.width = 2
>>> rect.width
2.0
```

```
# THIS WILL THROW EXCEPTION
```

```
>>> rect.width = "1.0"
TraitError: The 'width' trait of a
Rectangle instance must be a value of
type 'float', but a value of 1.0 was
specified.
```




Traits for Basic Python Types

Coercing Trait	Casting Trait	Python Type	Default Value
<code>Bool</code>	<code>CBool</code>	<code>bool</code>	<code>False</code>
<code>Complex</code>	<code>CComplex</code>	<code>complex</code>	<code>0+0j</code>
<code>Float</code>	<code>CFloat</code>	<code>float</code>	<code>0.0</code>
<code>Int</code>	<code>CInt</code>	<code>int</code>	<code>0</code>
<code>Long</code>	<code>CLong</code>	<code>long</code>	<code>0L</code>
<code>Str</code>	<code>CStr</code>	<code>str</code> or <code>unicode</code> (whichever assigned)	<code>' '</code>
<code>Unicode</code>	<code>CUnicode</code>	<code>unicode</code>	<code>u' '</code>



Derived properties

```
from enthought.traits.api import \
    HasTraits, Float, Property

class Rectangle(HasTraits):
    """ Rectangle class with
        read-only area property.
    """
    # Width of the rectangle
    width = Float(1.0)
    # Height of the rectangle
    height = Float(2.0)

    # The area of the rectangle
    # Defined as a property.
    area = Property
    # specially named method
    # automatically associated
    # with area.
    def _get_area(self):
        return self.width * self.height
```

Demo Code

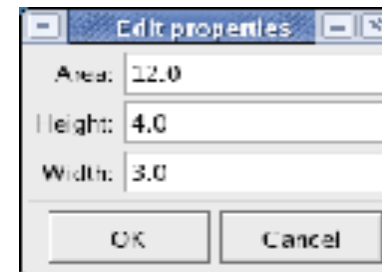
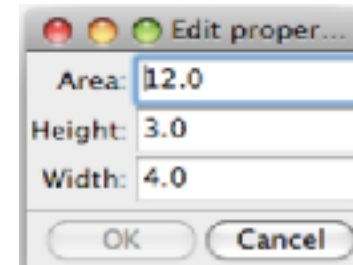
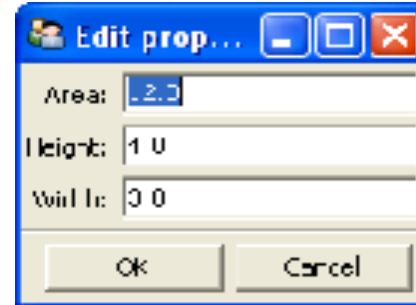
```
>>> rect = Rectangle(width=2.0,
                       height=3.0)

>>> rect.area
6.0
>>> rect.width = 4.0
>>> rect.area
8.0
```



Traits UI - Default Views

```
>>> rect = Rectangle(width=3.0, height = 4.0)  
# Create a UI to edit the traits of the object.  
>>> rect.edit_traits()
```

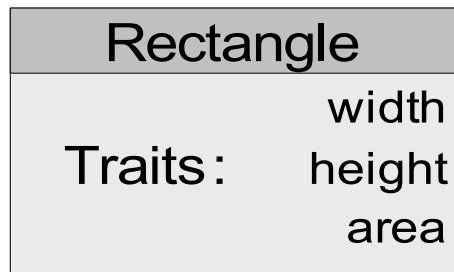




Trait Listeners

HasTraits Object

All traits automatically support the Listener Pattern



Listener Functions and Methods

Listeners are called in order whenever the 'width' trait changes





Dynamic Trait Notification

```
class Amplifier(HasTraits):  
    """ Guitar Amplifier Model  
    """  
  
    # Volume setting for the amplifier.  
    volume = Range(0.0, 11.0, default=5.0)  
  
def printer(value):  
    print "new value:", value
```

Demo Code

```
>>> spinal_tap = Amplifier()  
# In the following, name can also be a list of trait names  
>>> spinal_tap.on_trait_change(printer, name='volume')  
>>> spinal_tap.volume = 11.0  
new value: 11.0
```



@on_trait_change decorator

```
from enthought.traits.api import HasTraits, Range, on_trait_change
```

```
class Amplifier(HasTraits):  
    """ Guitar Amplifier Model  
    """  
  
    volume = Range(0.0, 11.0, value=5.0)  
    reverb = Range(0, 10.0, value=5.0)  
  
    # The on_trait_change decorator can listen to multiple traits  
    # Note the "list" of traits is specified as a string.  
    @on_trait_change('reverb, volume')  
    def update(self, name, value):  
        print 'trait %s updated to %s' % (name, value)
```

Demo Code

```
>>> spinal_tap = Amplifier()  
>>> spinal_tap.volume = 11.0  
trait volume updated to 11.0  
>>> spinal_tap.reverb = 2.0  
trait reverb updated to 2.0
```



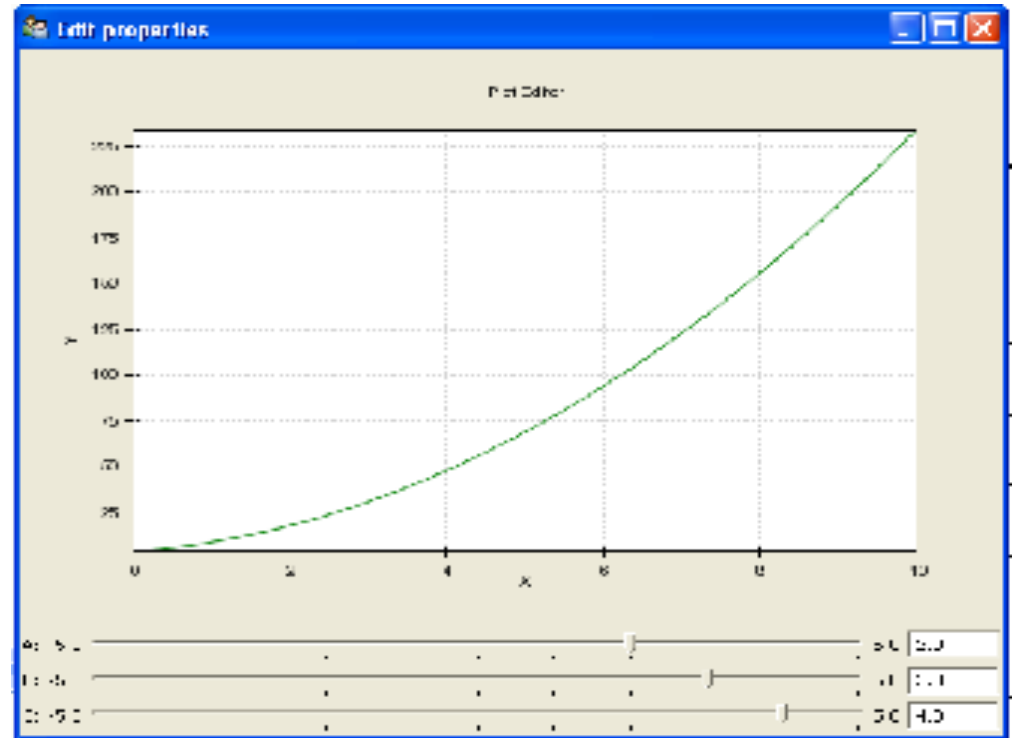
UI Demos

Table Demo

Retired	First	Last	Gender
<input checked="" type="checkbox"/>	Roh	One	male
<input type="checkbox"/>	John	Smith	male
<input type="checkbox"/>	Sally	Jones	female
<input type="checkbox"/>			

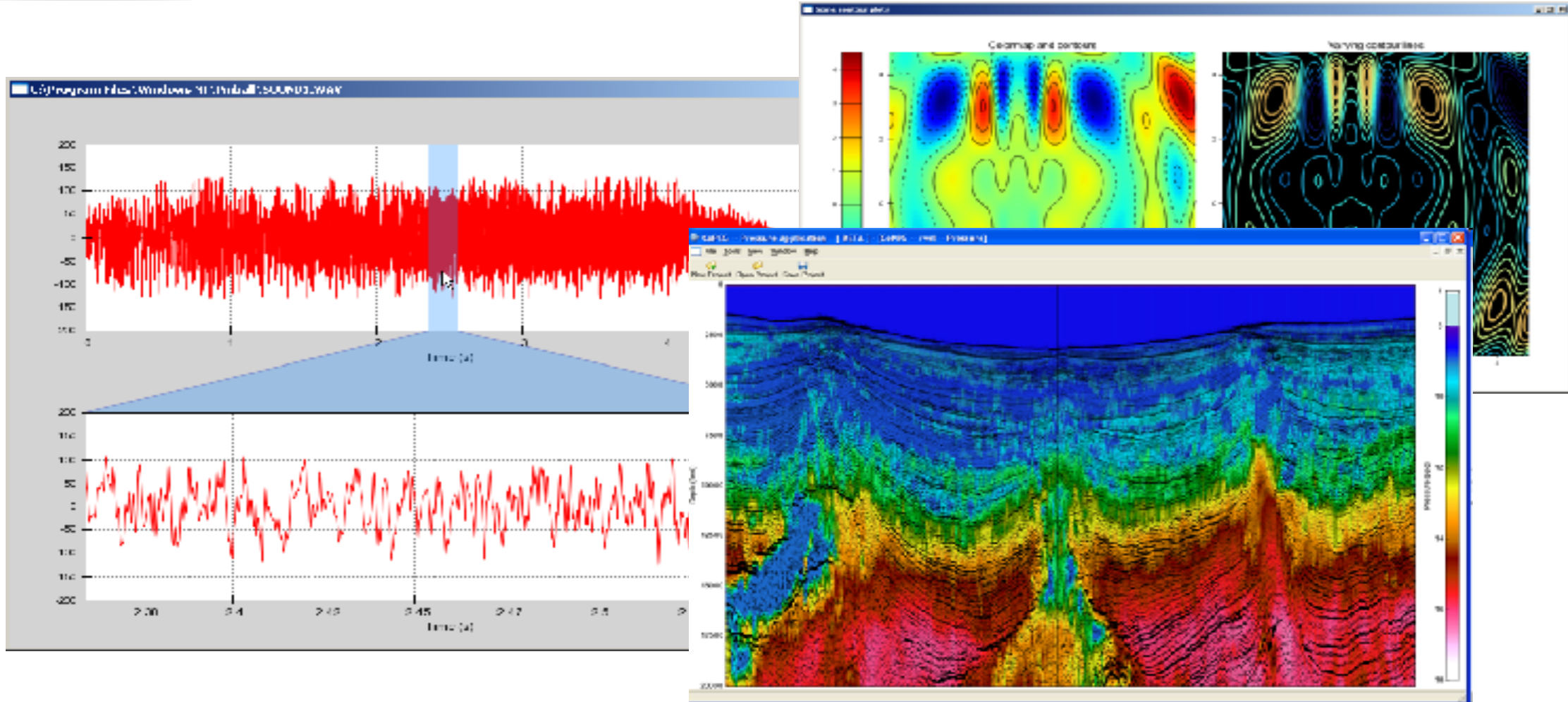
Buttons: OK, Cancel

Polynomial Demo





Chaco: Interactive Graphics





Contexts with Events

Code Block

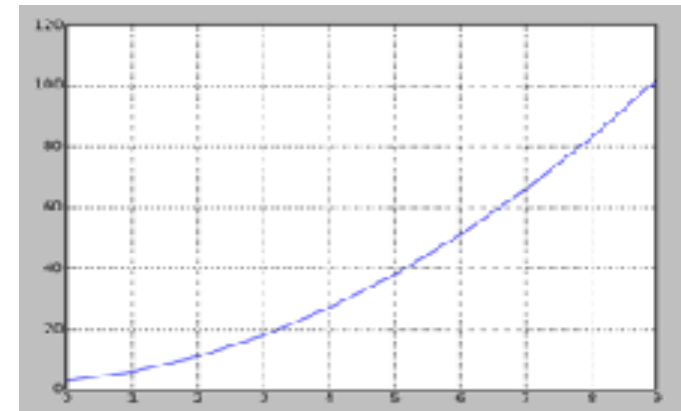
```
a=1  
b=2  
c=3  
y = a*x**2+b*x+c
```

Context

```
x: array( 0...9 )  
a: 1  
b: 2  
c: 3  
y: array( 3...102 )
```



Events Fire
when data
changes

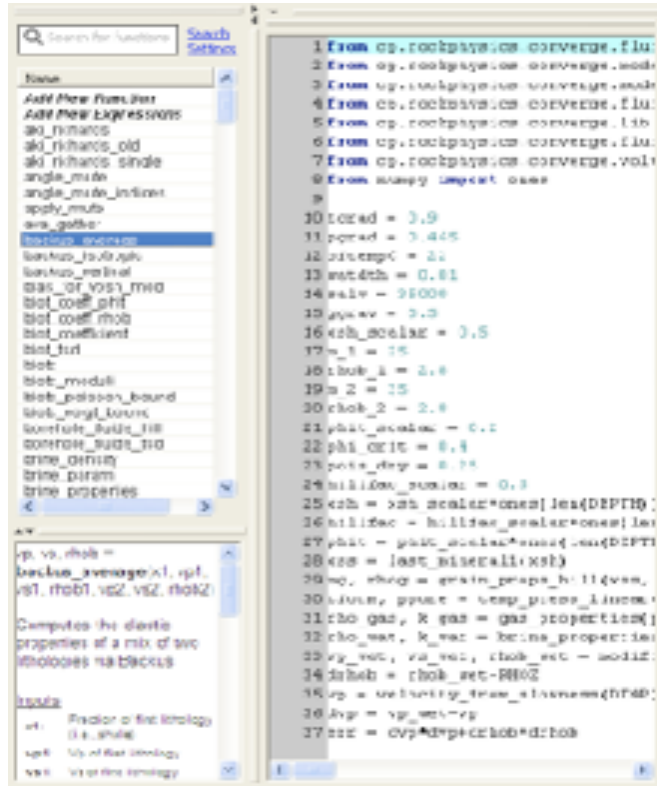


Updating Data View

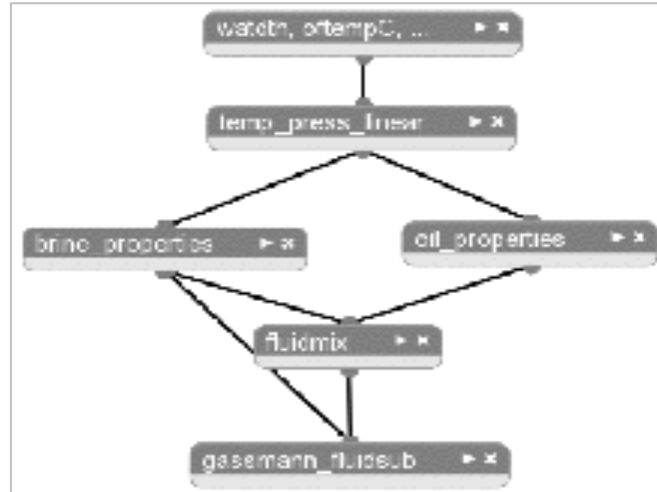


Three Classes of Users

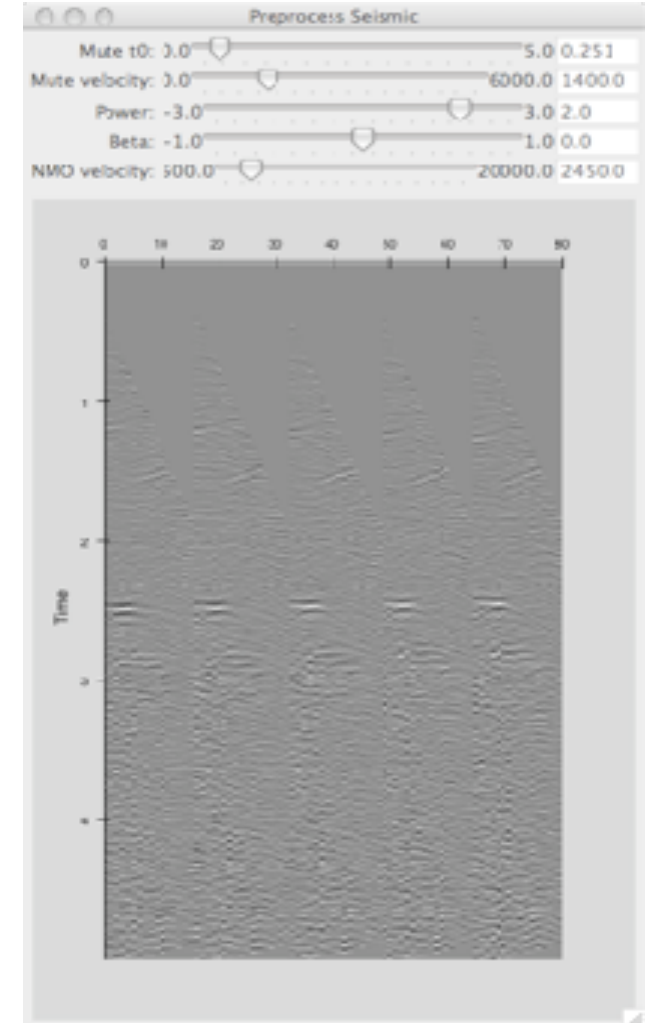
EXPERT



EXPERIENCED



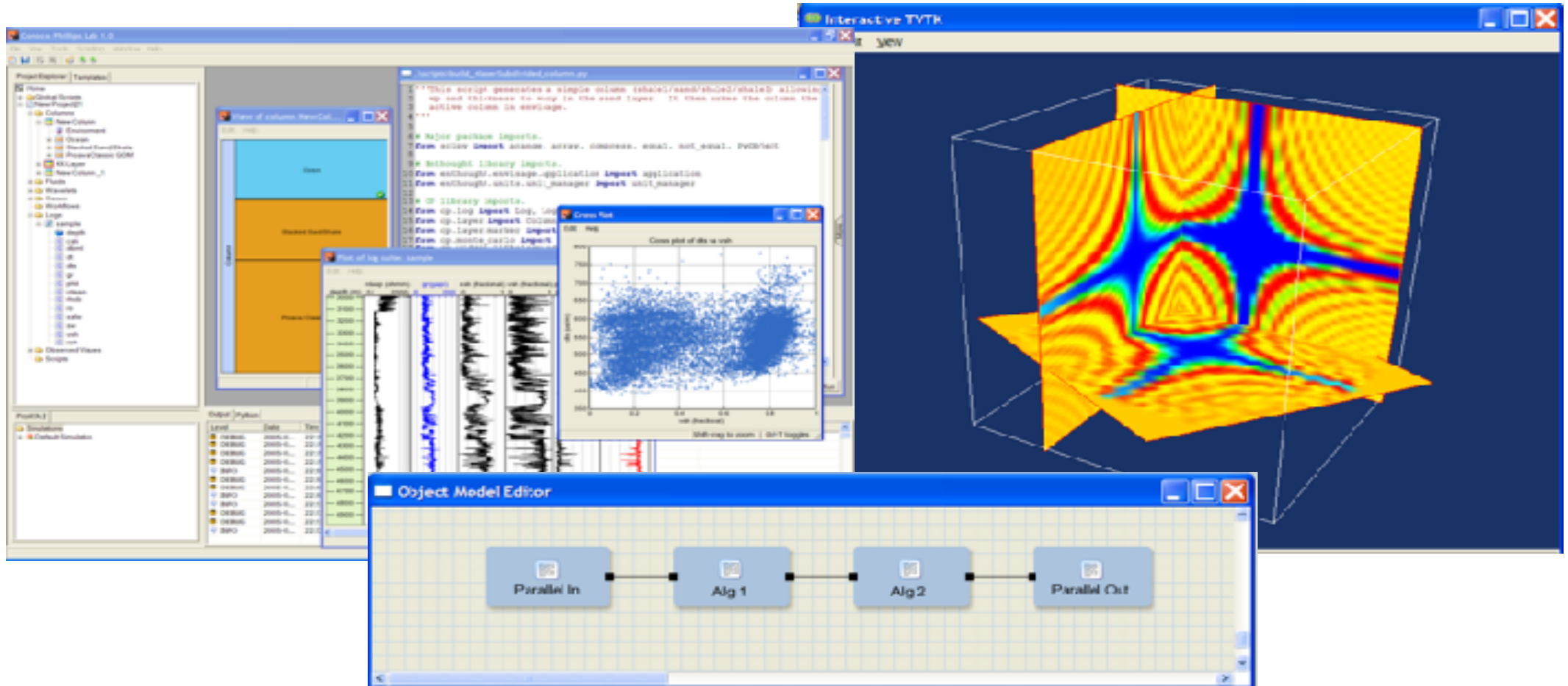
NOVICE





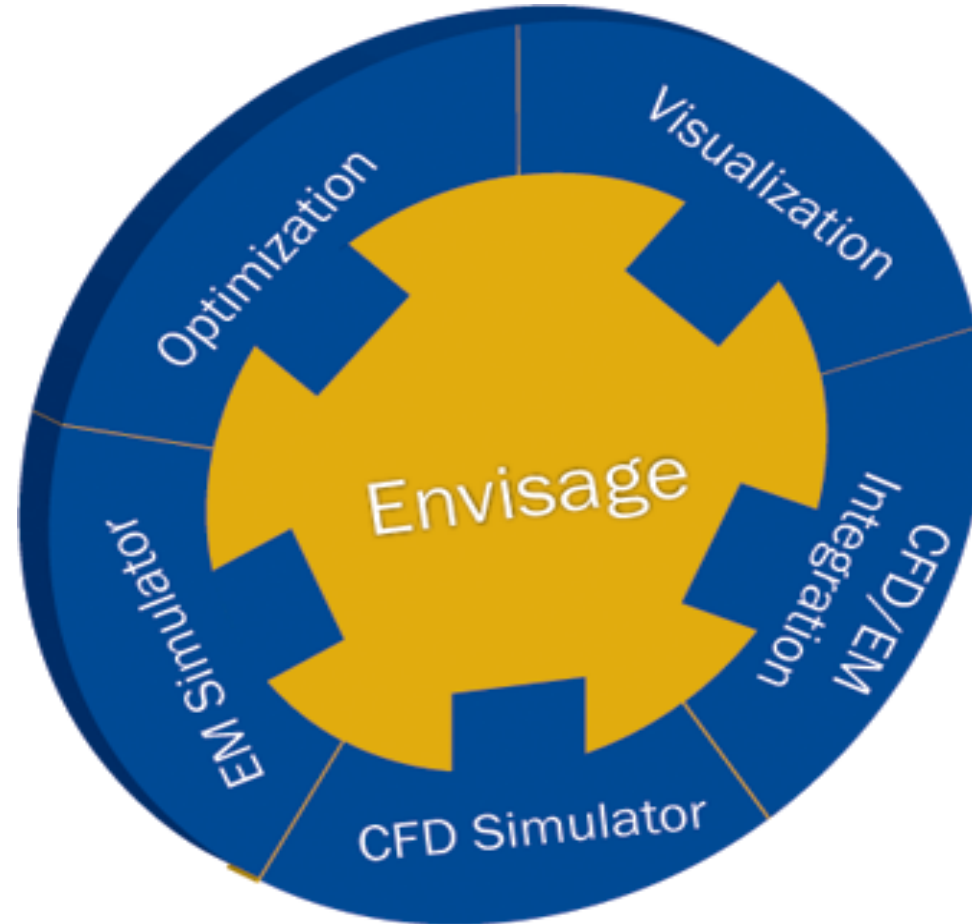
Envisage Application Framework

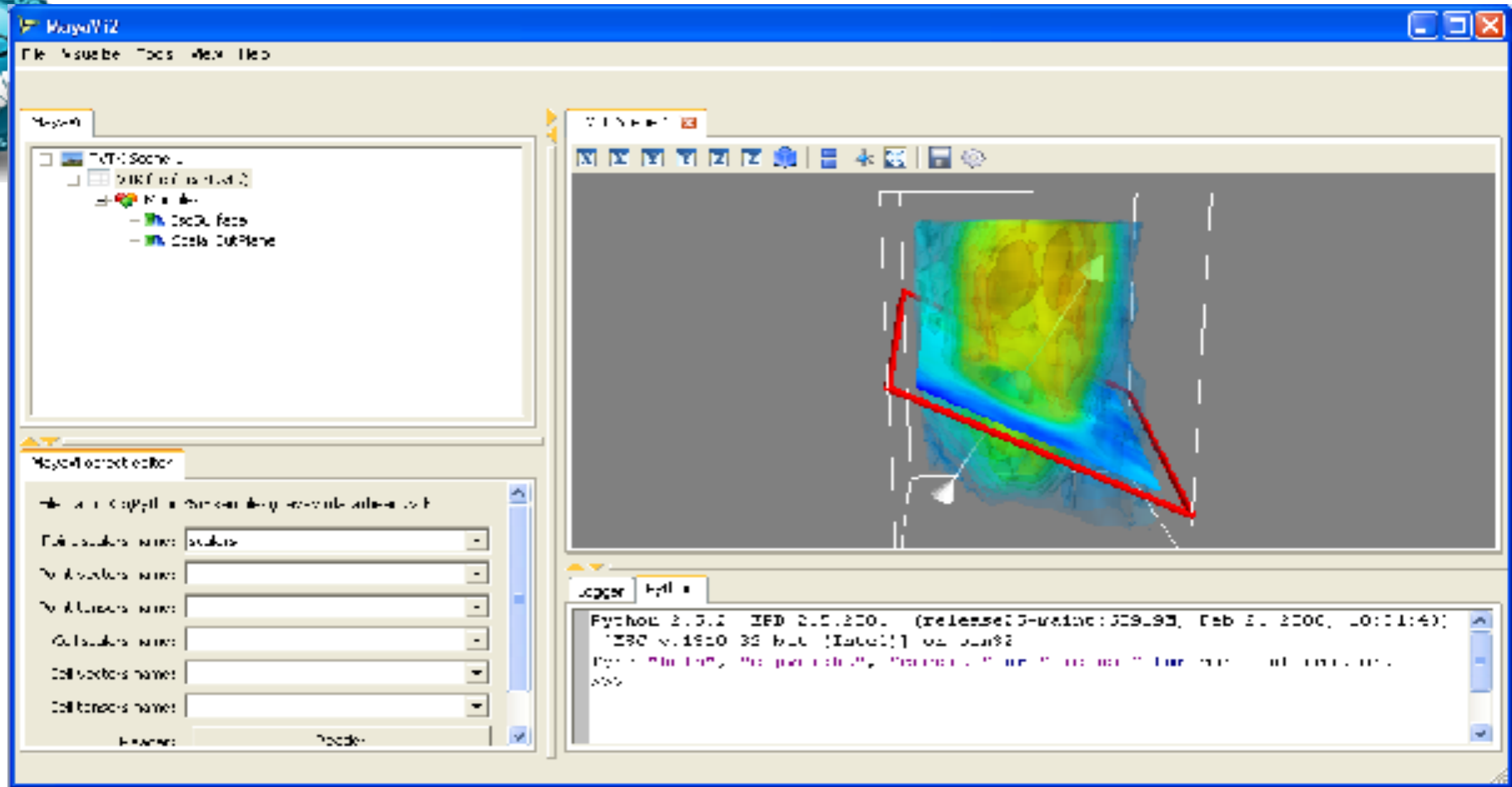
- Extensible
- Scriptable
- “Humane” Interface Tools built-in
- Easy Deployment





Multiple Plug-ins. One Application





Rich Client App (Geophysics, Finance, Etc)

Testing Framework Scripting Interface

Data Display

Equipment Interface

Compliance Tools

Scientific Algorithms

Database Access

Chaco Plotting

UI Elements





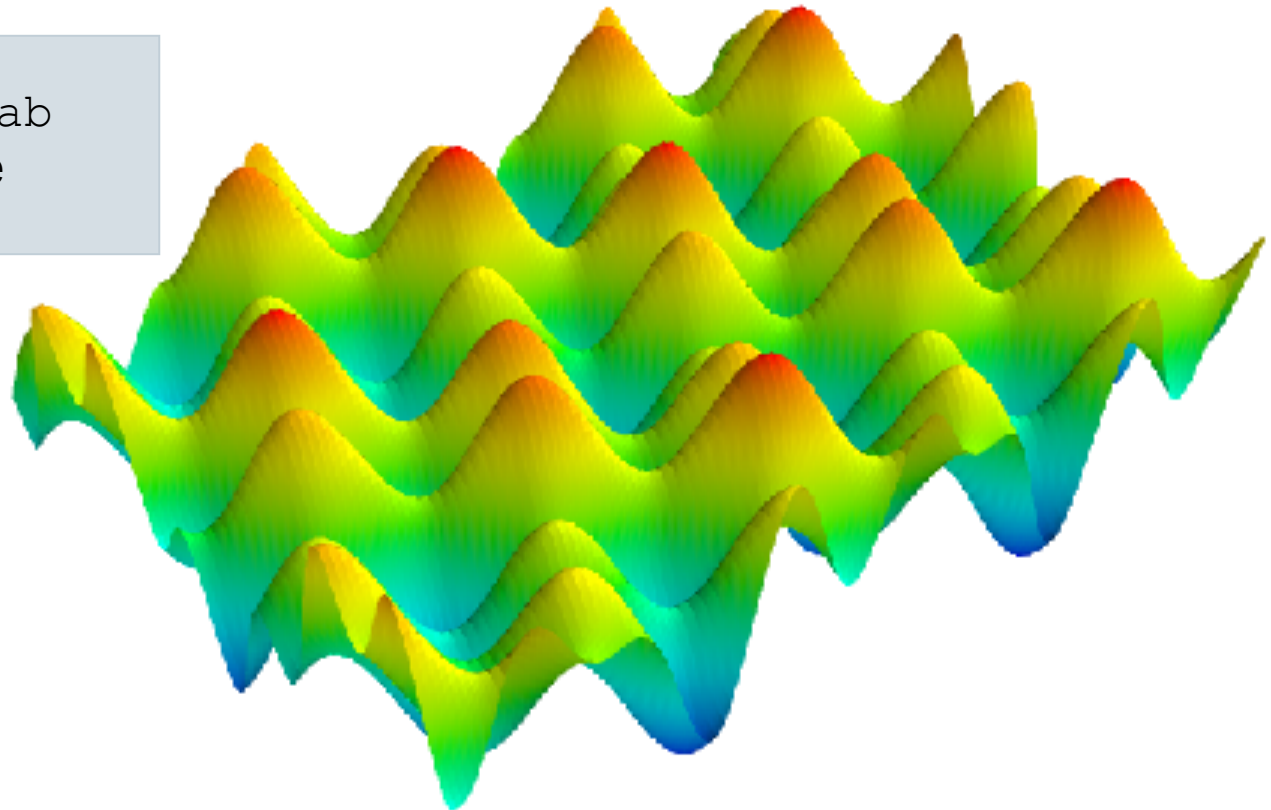
3D Visualization

```
C:\ ipython -wthread
```

```
>>> from enthought.mayavi import mlab
```



matplotlib also has an mlab namespace. Be sure you are using the one from `enthought.mayavi`





One example

```
# create arrays
```

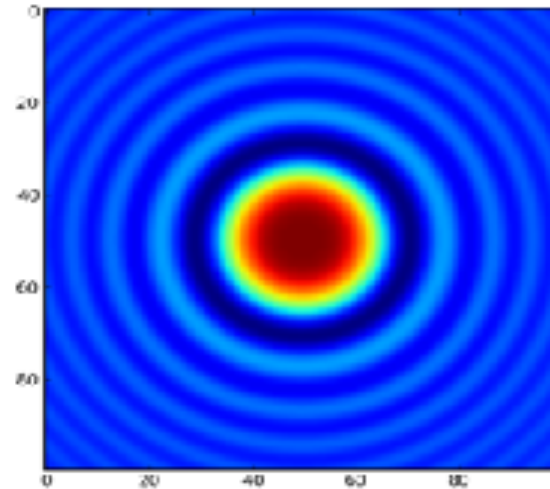
```
x, y = mgrid[-5:5:100j,-5:5:100j]
```

```
r = x**2 + y**2
```

```
z = sin(r)/r
```

```
# plot with pylab
```

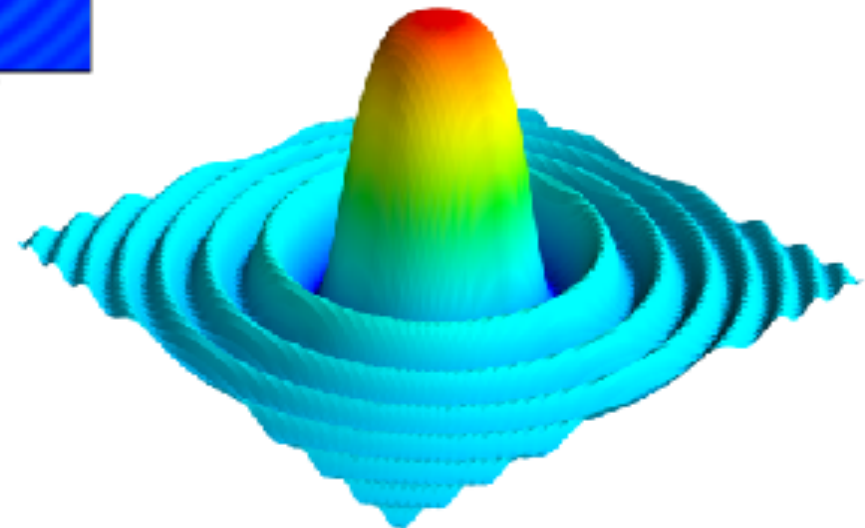
```
imshow(z)
```



```
# plot with mayavi
```

```
from enthought.mayavi import mlab
```

```
mlab.surf(50*z)
```



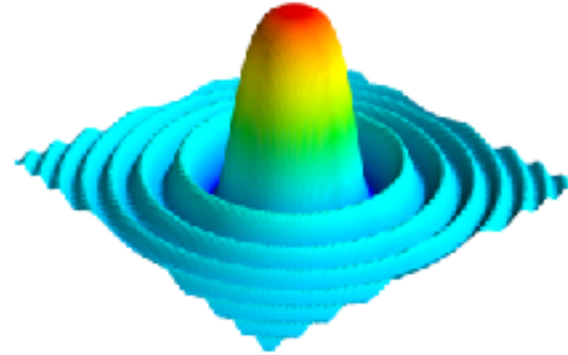


Plotting commands



0D data

`mlab.points3d(x, y, z)`



2D data

`mlab.surf(x, y, z)`



3D data

`mlab.contour3d(x, y, z)`



1D data

`mlab.plot3d(x, y, z)`



Vector field

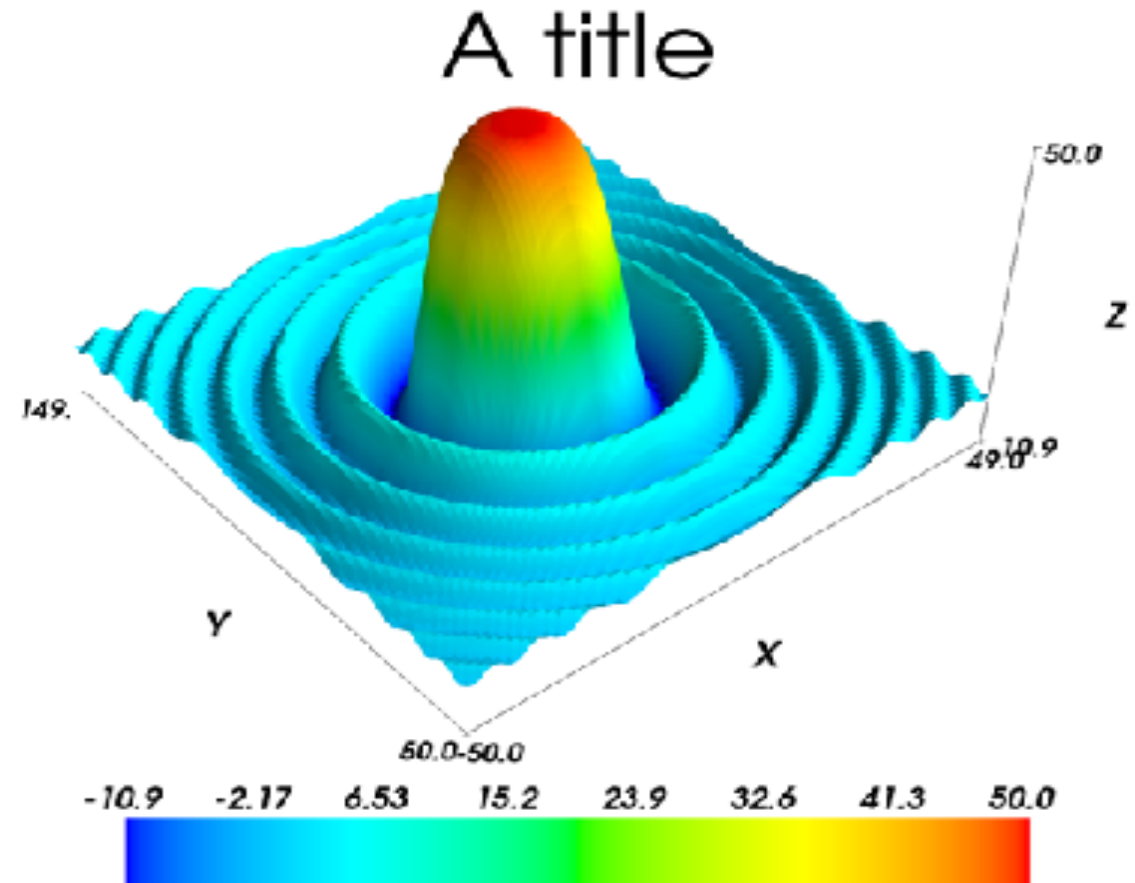
`mlab.quiver(x, y, z, u, v, w)`



Figure decorations

- `mlab.title('A title')`
- `mlab.axes()`
- `mlab.colorbar()`

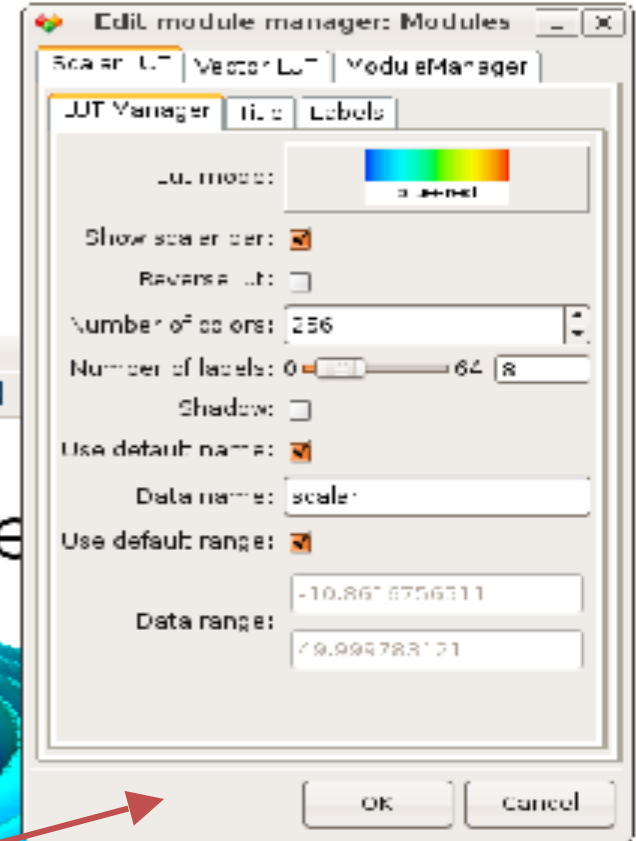
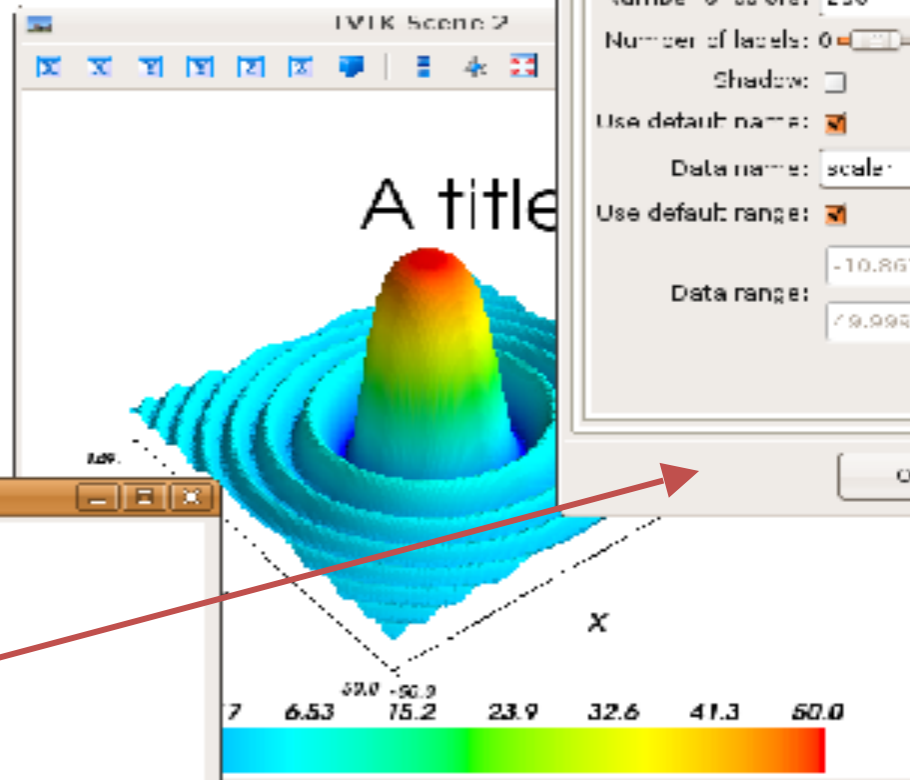
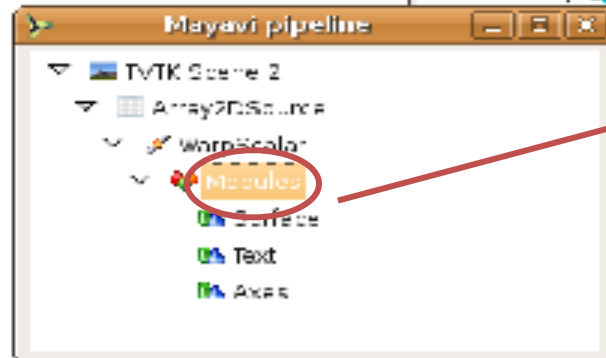
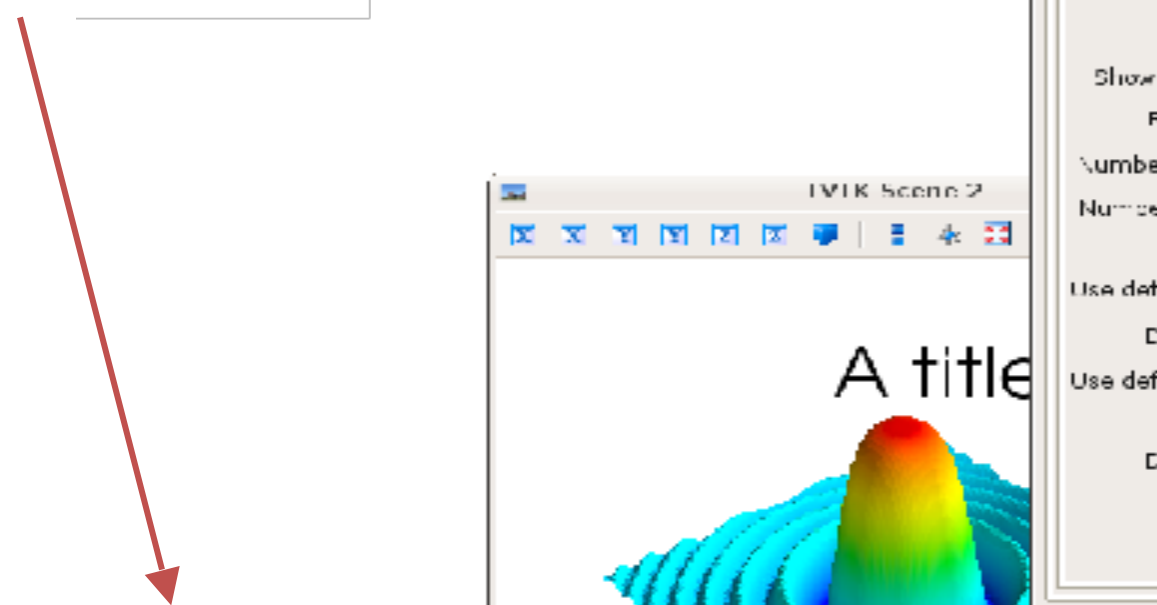
- `mlab.clf()`
- `mlab.figure()`
- `mlab.gcf()`





Graphical User Interface

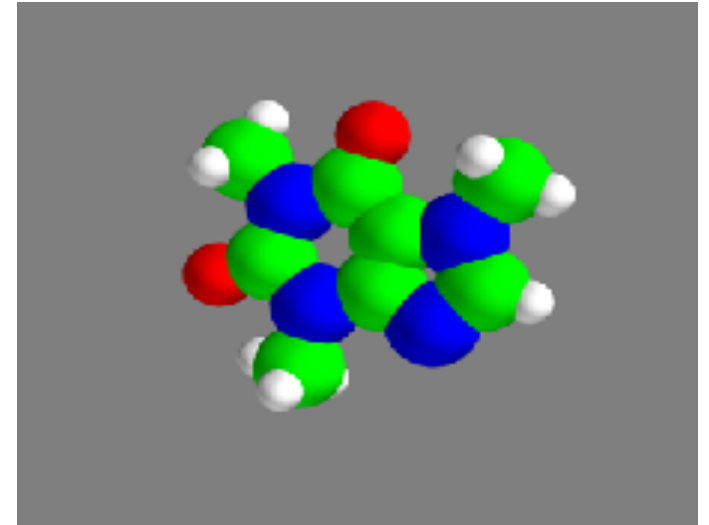
```
mlab.show_pipeline()
```





Examples and Demos

`mlab.test_points3d()`
`mlab.test_plot3d()`
`mlab.test_surf()`
`mlab.test_contour3d()`
`mlab.test_quiver3d()`



`mlab.test_molecule()`
`mlab.test_flow()`
`mlab.test_mesh()`



Use ?? in IPython to look at the source code of these examples.



Thank You